

A) Summary statistics for a sample :

		2D Flexural strength					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	17	16	15	16	15	17
Minimum value	X _{min} = X ₁	3,7	3,87	3,88	3,70	3,70	3,70
Maximum value	X _{max} = X _p	4,57	4,57	4,57	4,49	4,43	4,57
Range of sample R = difference L _{m95%} - L _{m95%}	X _{max} - X _{min} ΔL _{95%}	0,87 1,01	0,70	0,69	0,79	0,73	0,87 1,01
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	3,476					3,476
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	3,586					3,586
Lower Irwin confidence limit (for P=95%)	X _{minIw1-5%}	3,566					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	3,402	3,481				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	3,467	3,54				
Average (arithmetic mean) $\bar{x} = 1/p \sum(x_i) =$		4,091	4,116	4,132	4,061	4,033	4,091
Precision of a measure of the mean (for P=95%)	± ε	0,126	0,131	0,136	0,131	0,136	0,126
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	4,715			4,604		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	4,78			4,66		
Upper Irwin confidence limit (for P=99%)	X _{maxIw1-5%}	4,794					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	4,596					4,596
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	4,706					4,706
Standard deviation of a sample	S _{x,n-1}	0,2380	0,2227	0,2203	0,2102	0,1826	0,2380
Standard deviation	S _{x,0}	0,2309	0,2156	0,2129	0,2036	0,1764	0,2309
Coefficient of variation	v	5,8%	5,4%	5,3%	5,2%	4,5%	5,8%
Standard skewness	Sk _{est}	0,641	0,877	0,836	0,593	0,458	0,641
Standard kurtosis (exces)	Y ₂	-0,151	-0,263	-0,354	0,173	0,568	-0,151
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,120	2,132	2,145	2,132	2,145	2,120
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,584	2,603	2,625	2,603	2,625	2,584

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,318
	$\lambda_{calc,1,2}$	0,736
	$\lambda_{calc,n,n-1}$	0,346
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

	1,338	1,359	1,338	1,359
	0,046	0,000	0,835	0,964
	0,371	0,376	0,295	0,907
	1	1	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,643
Grubb $i=p$	G_p	2,013
Upper critical values	$G_{h,1\%}$	2,894
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.1	$G_{h,5\%}$	2,620
		1 ...
		1 ...
Grubb $i=1,2$	$G_{1,2}$	0,850
Grubb $i=p,p-1$	$G_{p,p-1}$	0,584
Lower critical values	$G_{d,1\%}$	0,299
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.2	$G_{d,5\%}$	0,382
		1 ...
		1 ...

	1,868
	2,422
	2,852

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 1 Value x_p is not outlier

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

1 Value x_1 is not biased
 1 Value x_p is not biased

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

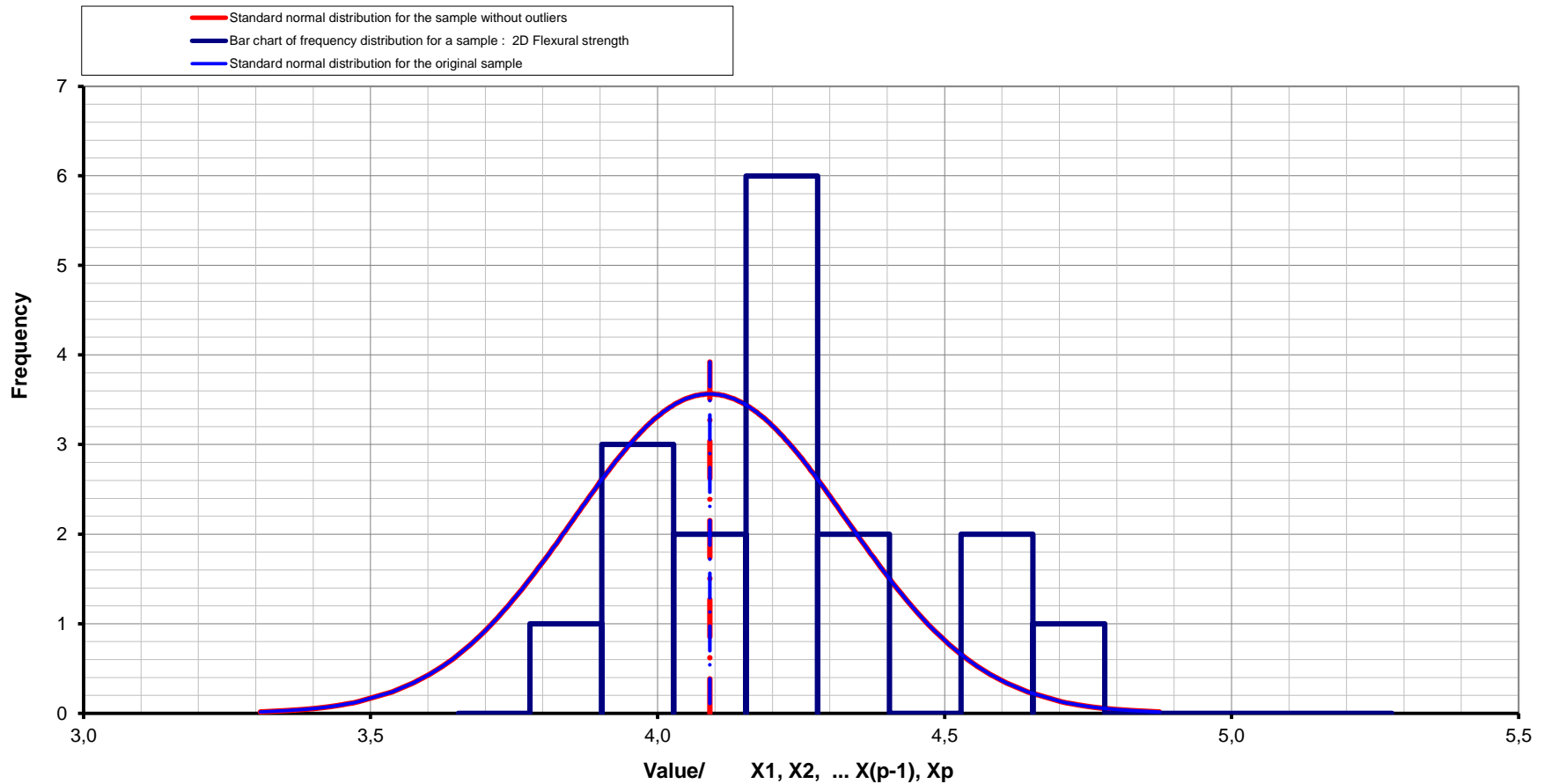
B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,195
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,092
Upper critical values	$Q_{v,\alpha,5\%}$	0,320
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

	0,014	0,000	0,215	0,233
	0,114	0,116	0,076	0,219
	0,329	0,338	0,329	0,338
	1	1	1	1
	1	1	1	1

Bar chart of frequency distribution for: 2D Flexural strength



A) Summary statistics for a sample :

		28D Flexural strength					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	17	16	15	16	15	16
Minimum value	$X_{min} = X_1$	6,37	7,28	7,52	6,37	6,37	7,28
Maximum value	$X_{max} = X_p$	9,04	9,04	9,04	8,71	8,48	9,04
Range of sample	$R = X_{max} - X_{min}$	2,67	1,76	1,52	2,34	2,11	1,76
difference $L_{m95\%} - L_{m98\%}$	$\Delta L_{95\%}$	2,592					1,916
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	6,457					6,972
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	6,740					7,183
Lower Irwin confidence limit (for P=95%)	$X_{minIw1-5\%}$	6,498					
Lower Grubbs confidence limit (for P=99%)	$X_{minG1-1\%}$	6,267	6,86				
Lower Grubbs confidence limit (for P=95%)	$X_{minG1-5\%}$	6,434	6,98				
Average (arithmetic mean)	$\bar{x} = 1/p \sum(x_i)$	8,036	8,141	8,198	7,974	7,925	8,141
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,324	0,336	0,350	0,336	0,350	0,247
Upper Grubbs confidence limit (for P=99%)	$X_{maxGp-5\%}$	9,638			9,453		
Upper Grubbs confidence limit (for P=95%)	$X_{maxGp-1\%}$	9,805			9,605		
Upper Irwin confidence limit (for P=99%)	$X_{maxIw1-5\%}$	9,492					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	9,332					9,099
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	9,615					9,31
Standard deviation of a sample	$S_{x,n-1}$	0,6113	0,4493	0,3998	0,5720	0,5562	0,4493
Standard deviation	$S_{x,0}$	0,593	0,435	0,3863	0,5539	0,5373	0,435
Coefficient of variation	v	7,6%	5,5%	4,9%	7,2%	7,0%	5,5%
Standard skewness	Sk_{est}	-1,134	0,005	0,329	-1,523	-1,677	0,005
Standard kurtosis (exces)	γ_2	2,513	0,069	0,073	3,167	3,520	0,069
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,120	2,132	2,145	2,132	2,145	2,132
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,584	2,603	2,625	2,603	2,625	2,603

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\lambda_{\alpha(n)}$	1,318
$\lambda_{\text{calc},1,2}$	1,535
$\lambda_{\text{calc},n,n-1}$	0,556

$x1^{**}$ 0 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

1,338	1,359	1,338	1,359
0,552	0,544	1,643	1,694
0,759	0,854	0,415	0,000

1 1 0 0
 1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	2,725
Grubb $i=p$	G_p	1,642
Upper critical values	$G_{h,1\%}$	2,894

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.1

$G_{h,5\%}$	2,620
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0 ...
 1 ...

3,942
1,864
2,852

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

0 $x1^{**}$ is the outlier
 1 Value x_p is not outlier
 0 $x1^*$ is the biased value
 1 Value x_p is not biased

Grubb $i=1,2$	$G_{1,2}$	0,424
Grubb $i=p,p-1$	$G_{p,p-1}$	0,821
Lower critical values	$G_{d,1\%}$	0,299

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.2

$G_{d,5\%}$	0,382
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1 ...
 1 ...

0,424
0,821
0,277

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values
 1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,341
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,124
Upper critical values	$Q_{v,\alpha,5\%}$	0,320

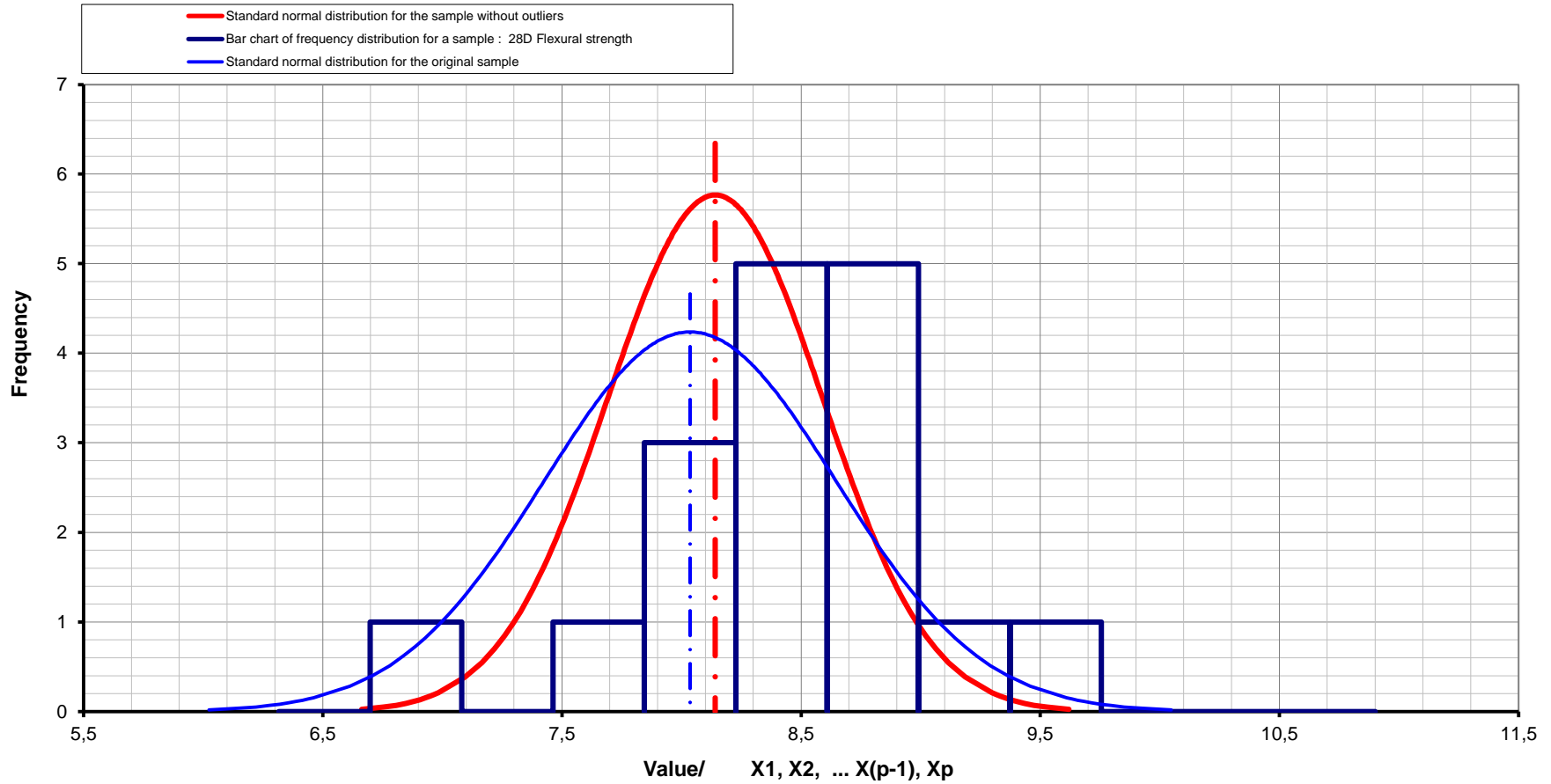
$x1^*$ is the biased value 0 ...
 Value x_p is not biased 1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

0,136	0,138	0,389	0,431
0,187	0,217	0,098	0,000
0,329	0,338	0,329	0,338

1 1 0 0
 1 1 1 1

Bar chart of frequency distribution for: 28D Flexural strength



A) Summary statistics for a sample :

		2D Compressive strength					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	17	16	15	16	15	16
Minimum value	X _{min} = X ₁	18,26	18,72	18,86	18,26	18,26	18,26
Maximum value	X _{max} = X _p	23,07	23,07	23,07	21,95	21,50	21,95
Range of sample R =	X _{max} - X _{min}	4,81	4,35	4,21	3,69	3,24	3,69
difference L _{m95%} - L _{m95%}	ΔL _{95%}	5,12					4,13
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	16,999					17,412
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	17,559					17,869
Lower Irwin confidence limit (for P=95%)	X _{minlw1-5%}	17,176					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	16,624	16,969				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	16,955	17,275				
Average (arithmetic mean) $\bar{x} =$	$1/p \sum(x_i) =$	20,119	20,235	20,336	19,934	19,800	19,934
Precision of a measure of the mean (for P=95%)	± ε	0,640	0,665	0,692	0,665	0,692	0,533
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	23,283			22,439		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	23,614			22,698		
Upper Irwin confidence limit (for P=99%)	X _{maxlw1-5%}	23,494					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	22,679					21,999
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	23,239					22,456
Standard deviation of a sample	S _{x,n-1}	1,2078	1,1451	1,1091	0,9690	0,8346	0,9690
Standard deviation	S _{x,0}	1,1717	1,1087	1,0715	0,9383	0,8063	0,9383
Coefficient of variation	v	6,0%	5,7%	5,5%	4,9%	4,2%	4,9%
Standard skewness	Sk _{est}	0,873	1,079	1,178	0,327	-0,044	0,327
Standard kurtosis (exces)	Y ₂	1,071	1,336	1,522	0,201	0,051	0,201
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,120	2,132	2,145	2,132	2,145	2,132
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,584	2,603	2,625	2,603	2,625	2,603

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,318
	$\lambda_{calc,1,2}$	0,393
	$\lambda_{calc,n,n-1}$	0,956
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiace of 5%				
	1,338	1,359	1,338	1,359
	0,126	0,299	0,490	0,571
	1,010	1,045	0,480	1,302
	1	1	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,539
Grubb $i=p$	G_p	2,443
Upper critical values	$G_{h,1\%}$	2,894
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.1	$G_{h,5\%}$	2,620
		1 ...
		1 ...
Grubb $i=1,2$	$G_{1,2}$	0,836
Grubb $i=p,p-1$	$G_{p,p-1}$	0,474
Lower critical values	$G_{d,1\%}$	0,299
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.2	$G_{d,5\%}$	0,382
		1 ...
		1 ...

	1,725
	3,236
	2,852
	2,585
	1
	0
	1
	0
	0,836
	0,474
	0,277
	1
	1
	1
	0,360
	1
	1

Test for an afterelimination of one outlier based on a level of signifiace of 1%

1 Value x_1 is not outlier
 0 x_p^{**} is the outlier
Test for an afterelimination of one biased value based on a level of signifiace of 5%
 1 Value x_1 is not biased
 0 x_p^* is the biased value

Test for an afterelimination of two outliers based on a level of signifiace of 5%

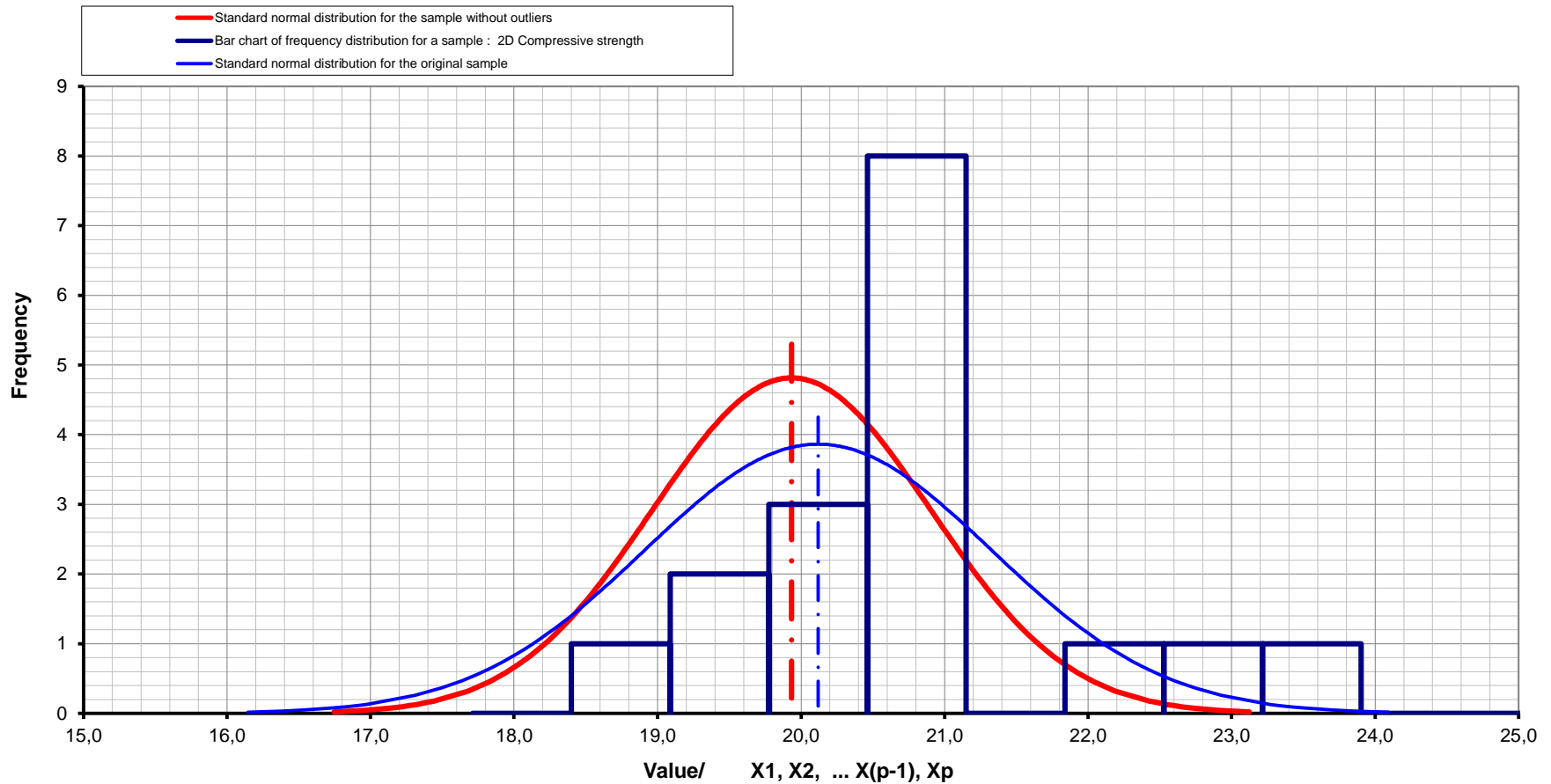
1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values
Test for an afterelimination of two biased values based on a level of signifiace of 5%
 1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,096
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,233
Upper critical values	$Q_{v,\alpha,5\%}$	0,320
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiace of 5%				
	0,032	0,076	0,125	0,142
	0,257	0,266	0,122	0,324
	0,329	0,338	0,329	0,338
	1	1	1	1
	1	1	1	1

Bar chart of frequency distribution for: 2D Compressive strength



A) Summary statistics for a sample :

28D Compressive strength							
	X1, X2, ... X(p-1), Xp		X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	17	16	15	16	15	17
Minimum value	$X_{min} = X_1$	47,46	48,00	48,16	47,46	47,46	47,46
Maximum value	$X_{max} = X_p$	53,38	53,38	53,38	52,95	52,34	53,38
Range of sample R = difference $L_{m95\%} - L_{m95\%}$	$X_{max} - X_{min}$	5,92	5,38	5,22	5,49	4,88	5,92
	$\Delta L_{95\%}$	7,236					7,236
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	45,780					45,78
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	46,571					46,571
Lower Irwin confidence limit (for P=95%)	$X_{minIw1-5\%}$	45,818					
Lower Grubbs confidence limit (for P=99%)	$X_{minG1-1\%}$	45,25	45,779				
Lower Grubbs confidence limit (for P=95%)	$X_{minG1-5\%}$	45,718	46,208				
Average (arithmetic mean) $\bar{x} = 1/p \sum (x_i) =$		50,189	50,359	50,517	49,989	49,792	50,189
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,904	0,939	0,978	0,939	0,978	0,904
Upper Grubbs confidence limit (for P=99%)	$X_{maxGp-5\%}$	54,66			53,981		
Upper Grubbs confidence limit (for P=95%)	$X_{maxGp-1\%}$	55,128			54,393		
Upper Irwin confidence limit (for P=99%)	$X_{maxIw1-5\%}$	55,132					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	53,807					53,807
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	54,598					54,598
Standard deviation of a sample	$S_{x,n-1}$	1,7065	1,6058	1,5293	1,5443	1,3738	1,7065
Standard deviation	$S_{x,0}$	1,6555	1,5549	1,4775	1,4953	1,3272	1,6555
Coefficient of variation	v	3,4%	3,2%	3,0%	3,1%	2,8%	3,4%
Standard skewness	Sk_{est}	0,327	0,430	0,483	0,247	0,056	0,327
Standard kurtosis (exces)	γ_2	-0,570	-0,573	-0,550	-0,473	-0,590	-0,570
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,120	2,132	2,145	2,132	2,145	2,120
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,584	2,603	2,625	2,603	2,625	2,584

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,318
	$\lambda_{calc,1,2}$	0,326
	$\lambda_{calc,n,n-1}$	0,260

Value x_1 is not outlier 1 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

1,338	1,359	1,338	1,359
0,103	0,589	0,361	0,407
0,277	0,291	0,408	0,618

1 1 1 1
 1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,599
Grubb $i=p$	G_p	1,870
Upper critical values	$G_{h,1\%}$	2,894

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.1

	$G_{h,5\%}$	2,620
		1 ...
		1 ...

Grubb $i=1,2$	$G_{1,2}$	0,797
Grubb $i=p,p-1$	$G_{p,p-1}$	0,643
Lower critical values	$G_{d,1\%}$	0,299

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.2

	$G_{d,5\%}$	0,382
		1 ...
		1 ...

1,805
2,196
2,852

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 1 Value x_p is not outlier

2,585
1 Value x_1 is not biased
1 Value x_p is not biased

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

0,797
0,643
0,277

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

0,360
1 Values x_1, x_2 are not outliers
1 Values x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of signifiacne of 5%

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,091
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,073
Upper critical values	$Q_{v,\alpha,5\%}$	0,320

Value x_1 is not biased 1 ...
 Value x_p is not biased 1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

0,030	0,167	0,098	0,111
0,080	0,082	0,111	0,168
0,329	0,338	0,329	0,338

1 1 1 1
 1 1 1 1

Bar chart of frequency distribution for: 28D Compressive strength

- Standard normal distribution for the sample without outliers
- Bar chart of frequency distribution for a sample : 28D Compressive strength
- Standard normal distribution for the original sample

