

A) Summary statistics for a sample :

2D Flexural strength						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
n	17	16	15	16	15	17
Minimum value	$x_{min} = x_1$	3,7	3,87	3,70	3,70	3,70
Maximum value	$x_{max} = x_p$	4,57	4,57	4,49	4,43	4,57
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{max} - x_{min}$	0,87	0,70	0,69	0,79	0,87
	$\Delta L_{95\%}$	1,01				1,01
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	3,476				3,476
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	3,586				3,586
	Lower Irwin confidence limit (for P=95%)	3,566				
	Lower Grubbs confidence limit (for P=99%)	3,402				
	Lower Grubbs confidence limit (for P=95%)	3,467				
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	4,091	3,481				4,091
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	3,54				0,126
	Upper Grubbs confidence limit (for P=99%)	4,715	4,116	4,061	4,033	
	Upper Grubbs confidence limit (for P=95%)	4,78	0,131	0,136	0,131	0,136
	Upper Irwin confidence limit (for P=99%)	4,794			4,604	
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	4,596				4,596
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	4,706				4,706
Standard deviation of a sample	$S_{x,n-1}$	0,2380	0,2227	0,2102	0,1826	0,2380
Standard deviation	$S_{x,0}$	0,2309	0,2156	0,2129	0,1764	0,2309
Coefficient of variation	v	5,8%	5,4%	5,3%	4,5%	5,8%
Standard skewness	Sk_{est}	0,641	0,877	0,836	0,593	0,641
Standard kurtosis (exces)	γ_2	-0,151	-0,263	-0,354	0,173	-0,151
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,120	2,132	2,145	2,132	2,120
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,584	2,603	2,625	2,603	2,584

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,318
	$\lambda_{\text{calc},1,2}$	0,736
	$\lambda_{\text{calc},n,n-1}$	0,346
Value x_1 is not outlier	1 ...	
Value x_p is not outlier	1 ...	

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

	1,338	1,359	1,338	1,359
	0,046	0,000	0,835	0,964
	0,371	0,376	0,295	0,907
1 ...	1	1	1	1
1 ...	1	1	1	1

B2) Tests by Grubbs for an afterelimination of outliers or biased values

Grubbs_i=1	G_1	1,643	
Grubbs_i=p	G_p	2,013	
Upper critical values	$G_{h,1\%}$	2,894	
for the Grubbs-test	1 ...		
according to ISO 5725-2,	1 ...		
clause 7.3.4.1	$G_{h,5\%}$	2,620	
	1 ...		
	1 ...		

		1,868	
		2,422	
		2,852	
		1 ...	
		1	

Test for an afterelimination of one outlier based on a level of signifiance of 1%

Value x_1 is not outlier

Value x_p is not outlier

Grubbs_i=p, p-1	$G_{p,p-1}$	0,584	
Lower critical values	$G_{d,1\%}$	0,299	
for the Grubbs-test	1 ...		
according to ISO 5725-2,	1 ...		
clause 7.3.4.1	$G_{d,5\%}$	0,382	
	1 ...		
	1 ...		

		0,850	
		0,584	
		0,277	
		1 ...	
		1	

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Grubbs_i=1,2	$G_{1,2}$	0,850	
Grubbs_i=p,p-1	$G_{p,p-1}$	0,584	
Lower critical values	$G_{d,1\%}$	0,299	
for the Grubbs-test	1 ...		
according to ISO 5725-2,	1 ...		
clause 7.3.4.2	$G_{d,5\%}$	0,382	
	1 ...		
	1 ...		

		0,850	
		0,584	
		0,277	
		1 ...	
		1	

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

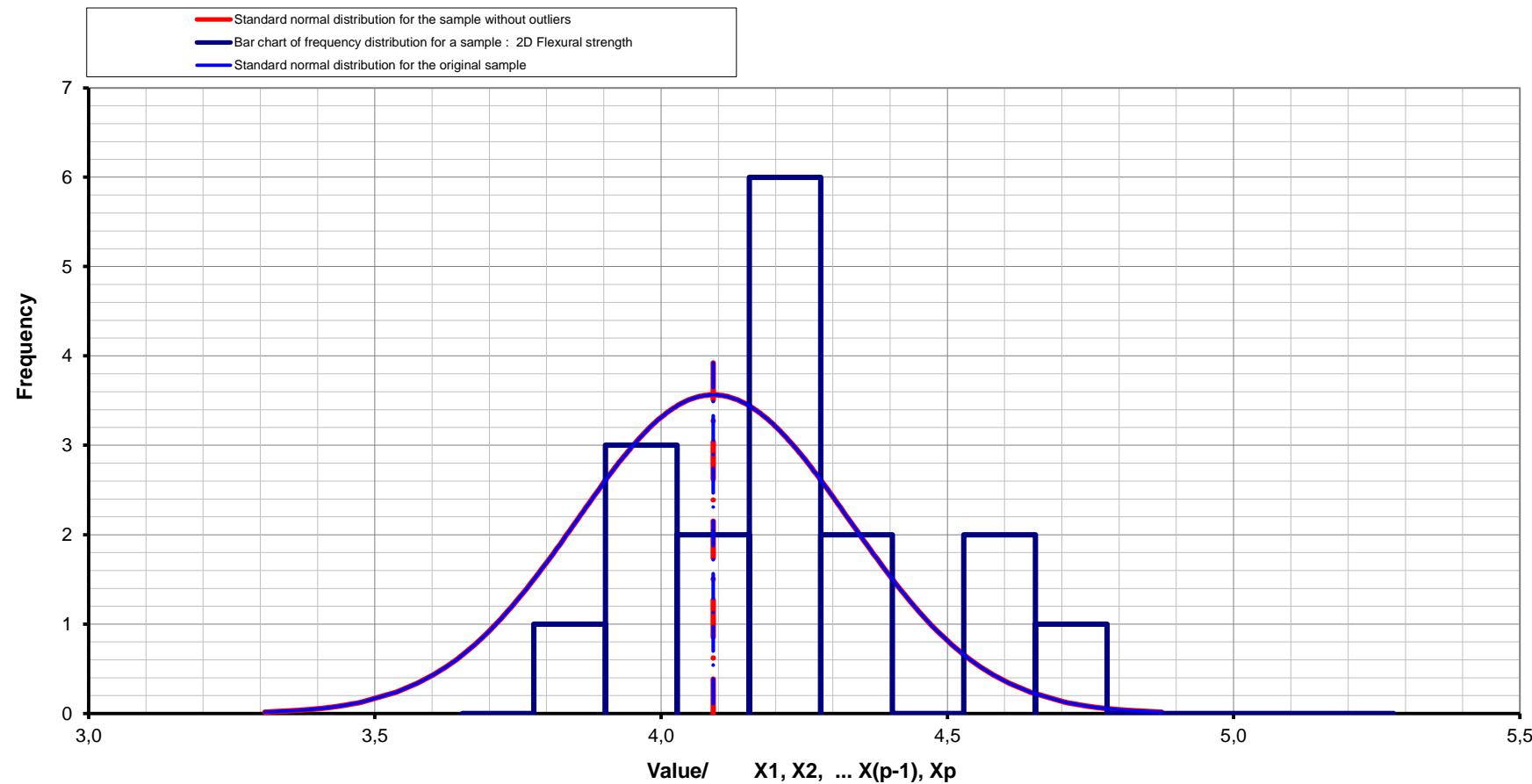
B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)	Q_1	0,195	
Dixon_i=p, ... ($x_p - x_{(p-1)}$)	Q_p	0,092	
Upper critical values	$Q_{v,a,5\%}$	0,320	
Value x_1 is not biased	1 ...		
Value x_p is not biased	1 ...		

	0,014	0,000	0,215	0,233
	0,114	0,116	0,076	0,219
	0,329	0,338	0,329	0,338
1 ...	1	1	1	1
1 ...	1	1	1	1

Bar chart of frequency distribution for:

2D Flexural strength



A) Summary statistics for a sample :

28D Flexural strength						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
n	17	16	15	16	15	16
Minimum value	6,37	7,28	7,52	6,37	6,37	7,28
Maximum value	9,04	9,04	9,04	8,71	8,48	9,04
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	2,67	1,76	1,52	2,34	2,11	1,76
$\Delta L_{95\%}$	2,592					1,916
Lower confidence limits after elimination of outliers (for P=98%)	6,457					6,972
Lower confidence limits after elimination of outliers (for P=95%)	6,740					7,183
Lower Irwin confidence limit (for P=95%)	6,498					
Lower Grubbs confidence limit (for P=99%)	6,267					
Lower Grubbs confidence limit (for P=95%)	6,434					
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	8,036	8,141	8,198	7,974	7,925	8,141
Precision of a measure of the mean (for P=95%)	0,324	0,336	0,350	0,336	0,350	0,247
Upper Grubbs confidence limit (for P=99%)	9,638					
Upper Grubbs confidence limit (for P=95%)	9,805					
Upper Irwin confidence limit (for P=99%)	9,492					
Upper confidence limits after elimination of outliers (for P=95%)	9,332					9,099
Upper confidence limits after elimination of outliers (for P=98%)	9,615					9,31
Standard deviation of a sample	0,6113					
Standard deviation	Sx,0	0,4493	0,3998	0,5720	0,5562	0,4493
Coefficient of variation	v	0,435	0,3863	0,5539	0,5373	0,435
Standard skewness	Sk _{est}	5,5%	4,9%	7,2%	7,0%	5,5%
Standard kurtosis (exces)	γ ₂	-1,134	0,005	0,329	-1,523	-1,677
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,120	0,069	0,073	3,167	3,520
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,584	2,132	2,145	2,132	2,132
		2,603	2,625	2,603	2,625	2,603

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,318
$\lambda_{\text{calc},1,2}$	1,535
$\lambda_{\text{calc},n,n-1}$	0,556

x_1^{**} 0 ...
Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,338	1,359	1,338	1,359
0,552	0,544	1,643	1,694
0,759	0,854	0,415	0,000

1 1 0 0
1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G ₁	2,725
Grubb_i=p	G _p	1,642
Upper critical values	G _{h,1%}	2,894

for the Grubb-test
according to ISO 5725-2,
clause 7.3.4.1

G _{h,5%}	2,620
0
1

3,942
1,864
2,852

Test for an afterelimination of one outlier based on a level of signifiance of 1%

x1 ** is the outlier

Value x_p is not outlier

Grubb_i=1,2	G _{1,2}	0,424
Grubb_i=p,p-1	G _{p,p-1}	0,821
Lower critical values	G _{d,1%}	0,299

for the Grubb-test
according to ISO 5725-2,
clause 7.3.4.2

G _{d,5%}	0,382
0
1

0,424
0,821
0,277

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values x₁, x₂ are not outliers

Values x_p, x_{p-1} are not biased values

Dixon_i=1, ... (x ₂ -x ₁)	Q ₁	0,341
Dixon_i=p, ... (x _p -x _(p-1))	Q _p	0,124
Upper critical values	Q _{v,a,5%}	0,320

x1 * is the biased value

Value x_p is not biased

0,136	0,138	0,389	0,431
0,187	0,217	0,098	0,000
0,329	0,338	0,329	0,338

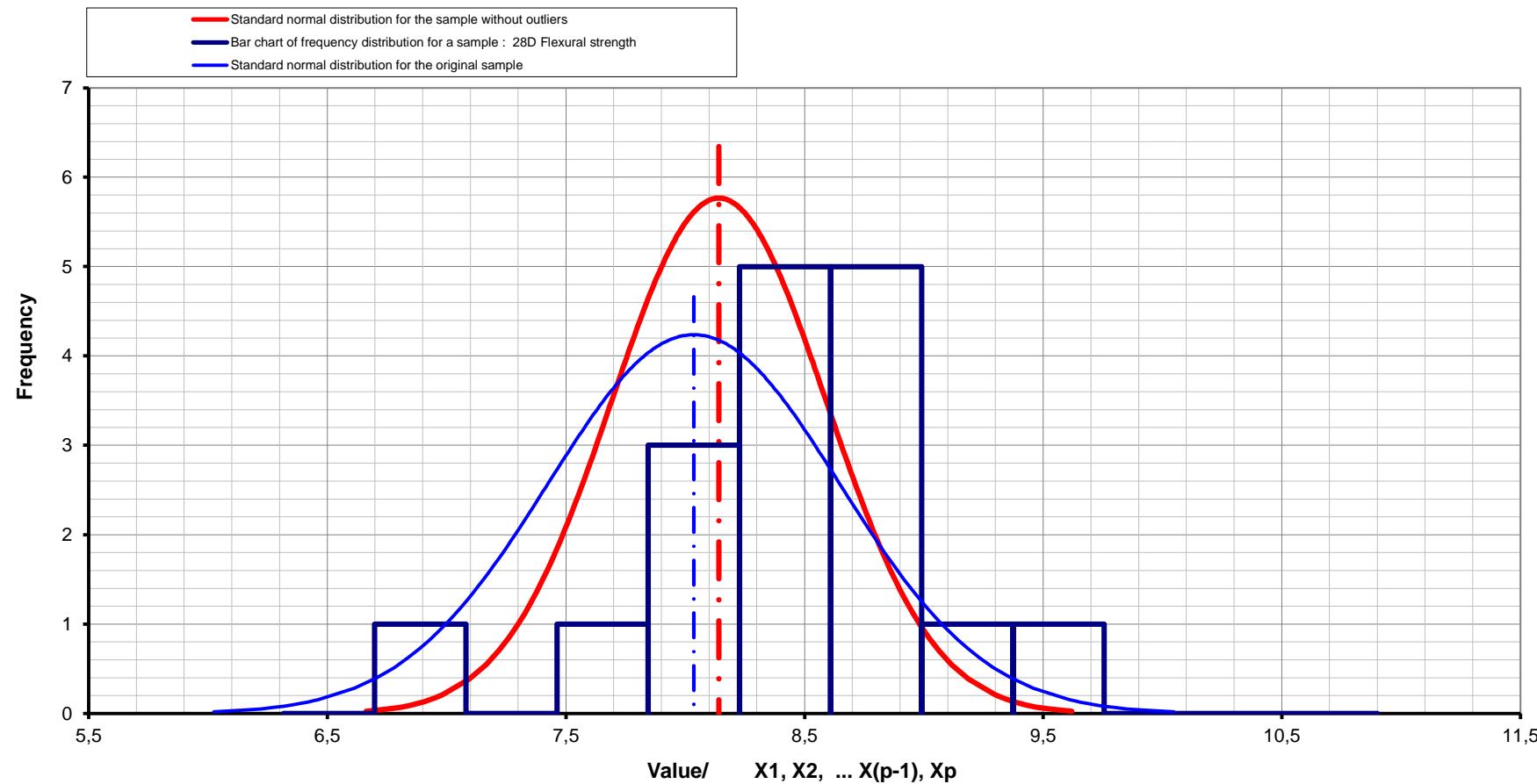
0 ... 1 0 0
1 ... 1 1 1

B3) Tests by Dixon for an afterelimination of outliers or biased values

Test for an afterelimination of one biased value based on a level of signifiance of 5%

Bar chart of frequency distribution for:

28D Flexural strength



A) Summary statistics for a sample :

2D Compressive strength						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 17	16	15	16	15	16
Minimum value	$x_{min} = x_1 = 18,3$	18,72	18,86	18,30	18,30	18,30
Maximum value	$x_{max} = x_p = 23,07$	23,07	23,07	21,95	21,50	21,95
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{max} - x_{min} = 4,77$ $\Delta L_{95\%} = 5,104$	4,35	4,21	3,65	3,20	3,65
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%} = 17,010$					4,112
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%} = 17,569$					17,427
Lower Irwin confidence limit (for P=95%)	$x_{min}l_{w1-5\%} = 17,181$					17,881
Lower Grubbs confidence limit (for P=99%)	$x_{min}G_{1-1\%} = 16,637$					
Lower Grubbs confidence limit (for P=95%)	$x_{min}G_{1-5\%} = 16,967$					
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} = 20,121$						
Precision of a measure of the mean (for P=95%)	$\pm \epsilon = 0,638$					
Upper Grubbs confidence limit (for P=99%)	$x_{max}G_{p-5\%} = 23,275$					
Upper Grubbs confidence limit (for P=95%)	$x_{max}G_{p-1\%} = 23,605$					
Upper Irwin confidence limit (for P=99%)	$x_{max}l_{w1-5\%} = 23,489$					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%} = 22,673$					21,993
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%} = 23,232$					22,447
Standard deviation of a sample	$s_{x,n-1} = 1,2040$					
Standard deviation	$s_{x,0} = 1,168$					
Coefficient of variation	$v = 6,0\%$	1,1451	1,1091	0,9645	0,8294	0,9645
Standard skewness	$Sk_{est} = 0,891$	1,1087	1,0715	0,9339	0,8013	0,9339
Standard kurtosis (exces)	$\gamma_2 = 1,079$	5,7%	5,5%	4,8%	4,2%	4,8%
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%} = 2,120$	1,079	1,178	0,351	-0,016	0,351
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%} = 2,584$	1,336	1,522	0,187	0,018	0,187
		2,132	2,145	2,132	2,145	2,132
		2,603	2,625	2,603	2,625	2,603

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,318
	$\lambda_{\text{calc},1,2}$	0,360
	$\lambda_{\text{calc},n,n-1}$	0,959
Value x_1 is not outlier	1 ...	
Value x_p is not outlier	1 ...	

Tests by Irwin for an afterelimination of outliers based on a level of significance of 5%

	1,338	1,359	1,338	1,359
	0,126	0,299	0,450	0,524
	1,010	1,045	0,482	1,310
1 ...	1	1	1	1
1 ...	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G_1	1,512	1,690
Grubb_i=p	G_p	2,449	3,248
Upper critical values	$G_{h,1\%}$	2,894	2,852
for the Grubb-test	1 ...	1	Value x_1 is not outlier
according to ISO 5725-2, clause 7.3.4.1	$G_{h,5\%}$	2,620	2,585
	1 ...	0	xp ** is the outlier
	1 ...	1	Value x_1 is not biased
	1 ...	0	xp * is the biased value
Grubb_i=1,2	$G_{1,2}$	0,842	0,842
Grubb_i=p,p-1	$G_{p,p-1}$	0,471	0,471
Lower critical values	$G_{d,1\%}$	0,299	0,277
for the Grubb-test	1 ...	1	Values x_1, x_2 are not outliers
according to ISO 5725-2, clause 7.3.4.2	$G_{d,5\%}$	0,382	0,360
	1 ...	1	Values x_1, x_2 are not outliers
	1 ...	1	Values x_p, x_{p-1} are not biased values

Test for an afterelimination of one outlier based on a level of significance of 1%

Value x_1 is not outlier
 xp ** is the outlier

Test for an afterelimination of one biased value based on a level of significance of 5%

Value x_1 is not biased
 xp * is the biased value

Test for an afterelimination of two outliers based on a level of significance of 5%

Values x_1, x_2 are not outliers
 Values x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of significance of 5%

Values x_1, x_2 are not outliers
 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

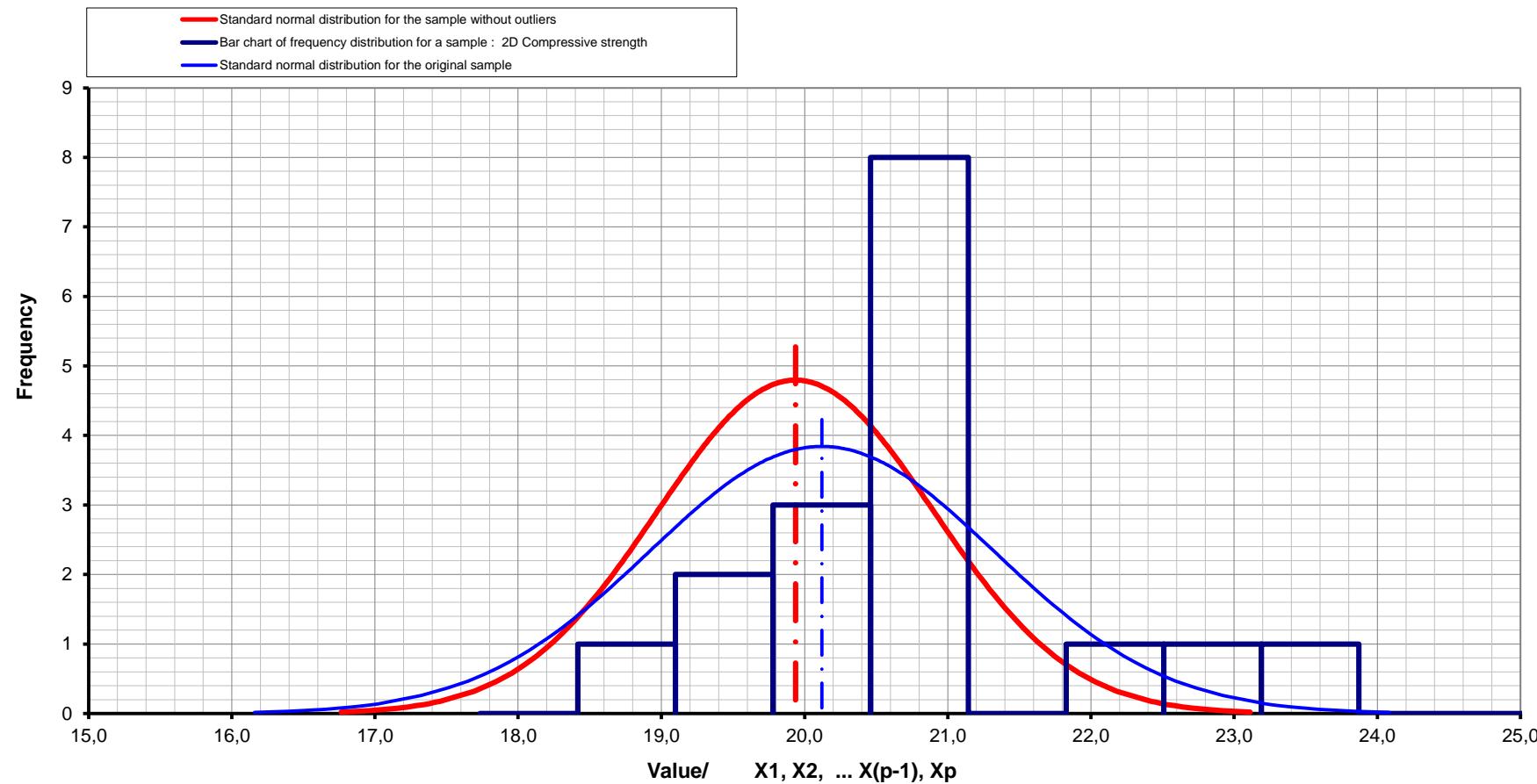
Dixon_i=1, ... (x_2-x_1)	Q_1	0,088	0,032
Dixon_i=p, ... ($x_p-x_{(p-1)}$)	Q_p	0,235	0,257
Upper critical values	$Q_{v,a,5\%}$	0,320	0,329
Value x_1 is not biased	1 ...	1	1
Value x_p is not biased	1 ...	1	1

Test for an afterelimination of one biased value based on a level of significance of 5%

	0,076	0,115	0,131
	0,266	0,123	0,328
	0,338	0,329	0,338
1 ...	1	1	1
1 ...	1	1	1

Bar chart of frequency distribution for:

2D Compressive strength



A) Summary statistics for a sample :

28D Compressive strength						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	17				17
Minimum value	$x_{\min} = x_1$	47,46				47,46
Maximum value	$x_{\max} = x_p$	53,38				53,38
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$	5,92				5,92
	$\Delta L_{95\%}$	7,236				7,236
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	45,780				45,78
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	46,571				46,571
	Lower Irwin confidence limit (for P=95%)	45,818				
	Lower Grubbs confidence limit (for P=99%)	45,25				
	Lower Grubbs confidence limit (for P=95%)	45,718				
Precision of a measure of the mean (for P=95%)	Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	50,189				50,189
	$\pm \epsilon$	0,904				0,904
	Upper Grubbs confidence limit (for P=99%)	54,66				
	Upper Grubbs confidence limit (for P=95%)	55,128				
	Upper Irwin confidence limit (for P=99%)	55,132				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	53,807				53,807
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	54,598				54,598
	Standard deviation of a sample $S_{x,n-1}$	1,7065				1,7065
	Standard deviation $S_{x,0}$	1,6555				1,6555
Coefficient of variation	v	3,4%				3,4%
	Standard skewness Sk_{est}	0,327				0,327
	Standard kurtosis (exces) γ_2	-0,570				-0,570
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,120				2,120
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,584				2,584
			2,132	2,145	2,132	2,145
			2,603	2,625	2,603	2,625

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,318
$\lambda_{\text{calc},1,2}$	0,326
$\lambda_{\text{calc},n,n-1}$	0,260

Value x_1 is not outlier 1 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,338	1,359	1,338	1,359
0,103	0,589	0,361	0,407
0,277	0,291	0,408	0,618

1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	1,599
G_p	1,870

Upper critical values

$G_{h,1\%}$	2,894
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for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.1

$G_{h,5\%}$	2,620
1 ...	1
1 ...	1

Lower critical values

$G_{1,2}$	0,797
$G_{p,p-1}$	0,643
$G_{d,1\%}$	0,299

for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.2

$G_{d,5\%}$	0,382
1 ...	1
1 ...	1

Test for an afterelimination of one outlier based on a level of signifiance of 1%

1,805
2,196
2,852

Value x_1 is not outlier

Value x_p is not outlier

Test for an afterelimination of one biased value based on a level of signifiance of 5%

1,105
1,496
2,585

Value x_1 is not biased

Value x_p is not biased

Test for an afterelimination of two outliers based on a level of signifiance of 5%

0,797
0,643
0,277

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of signifiance of 5%

0,360
0,360
0,360

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Q_1	0,091
Q_p	0,073
$Q_{v,a,5\%}$	0,320

Value x_1 is not biased	1 ...
Value x_p is not biased	1 ...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,030
0,080
0,329

Value x_1 is not biased

Value x_p is not biased

0,167
0,082
0,338

Value x_1 is not biased

Value x_p is not biased

0,098
0,111
0,329

Value x_1 is not biased

Value x_p is not biased

0,111
0,168
0,338

Value x_1 is not biased

Value x_p is not biased

Bar chart of frequency distribution for:

28D Compressive strength

