

A) Summary statistics for a sample :

		Specific surface (Blaine)					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	13	12	11	12	11	12
Minimum value	X _{min} = X ₁	466,8	476,60	478,20	466,80	466,80	476,60
Maximum value	X _{max} = X _p	524,1	524,10	524,10	515,00	512,40	524,10
Range of sample	R = X _{max} - X _{min}	57,3	47,50	45,90	48,20	45,60	47,50
difference L _{m95%} - L _{m95%}	ΔL _{95%}	73,22					61,44
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	455,64					465,57
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	464,07					472,79
Lower Irwin confidence limit (for P=95%)	X _{minIw1-5%}	453,83					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	455,33	466,71				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	459,32	469,84				
Average (arithmetic mean)	$\bar{x} = 1/p \sum(x_i)$	500,68	503,51	505,95	498,73	497,25	503,51
Precision of a measure of the mean (for P=95%)	± ε	10,57	11,15	11,84	11,15	11,84	9,26
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	542,04			537,17		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	546,03			540,73		
Upper Irwin confidence limit (for P=99%)	X _{maxIw1-5%}	537,77					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	537,29					534,23
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	545,72					541,45
Standard deviation of a sample	S _{x,n-1}	16,801	13,959	11,634	15,935	15,826	13,959
Standard deviation	S _{x,0}	16,142	13,364	11,092	15,257	15,089	13,364
Coefficient of variation	v	3,4%	2,8%	2,3%	3,2%	3,2%	2,8%
Standard skewness	Sk _{est}	-0,929	-0,973	-1,155	-1,109	-1,058	-0,973
Standard kurtosis (exces)	Y ₂	0,036	0,710	2,992	-0,112	-0,370	0,710
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,179	2,201	2,228	2,201	2,228	2,201
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,681	2,718	2,764	2,718	2,764	2,718

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,411
	$\lambda_{\text{calc},1,2}$	0,607
	$\lambda_{\text{calc},n,n-1}$	0,564
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

	1,441	1,477	1,441	1,477
	0,120	1,785	0,642	0,649
	0,681	0,820	0,170	0,139
	1	0	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	2,017
Grubb $i=p$	G_p	1,394
Upper critical values	$G_{h,1\%}$	2,699
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.1	$G_{h,5\%}$	2,462
		1 ...
		1 ...

	2,630
	1,592
	2,636

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

	1	Value x_1 is not outlier
	1	Value x_p is not outlier
	0	x_1^* is the biased value
	1	Value x_p is not biased

Grubb $i=1,2$	$G_{1,2}$	0,472
Grubb $i=p,p-1$	$G_{p,p-1}$	0,874
Lower critical values	$G_{d,1\%}$	0,202
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.2	$G_{d,5\%}$	0,284
		1 ...
		1 ...

	0,472
	0,874
	0,174

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

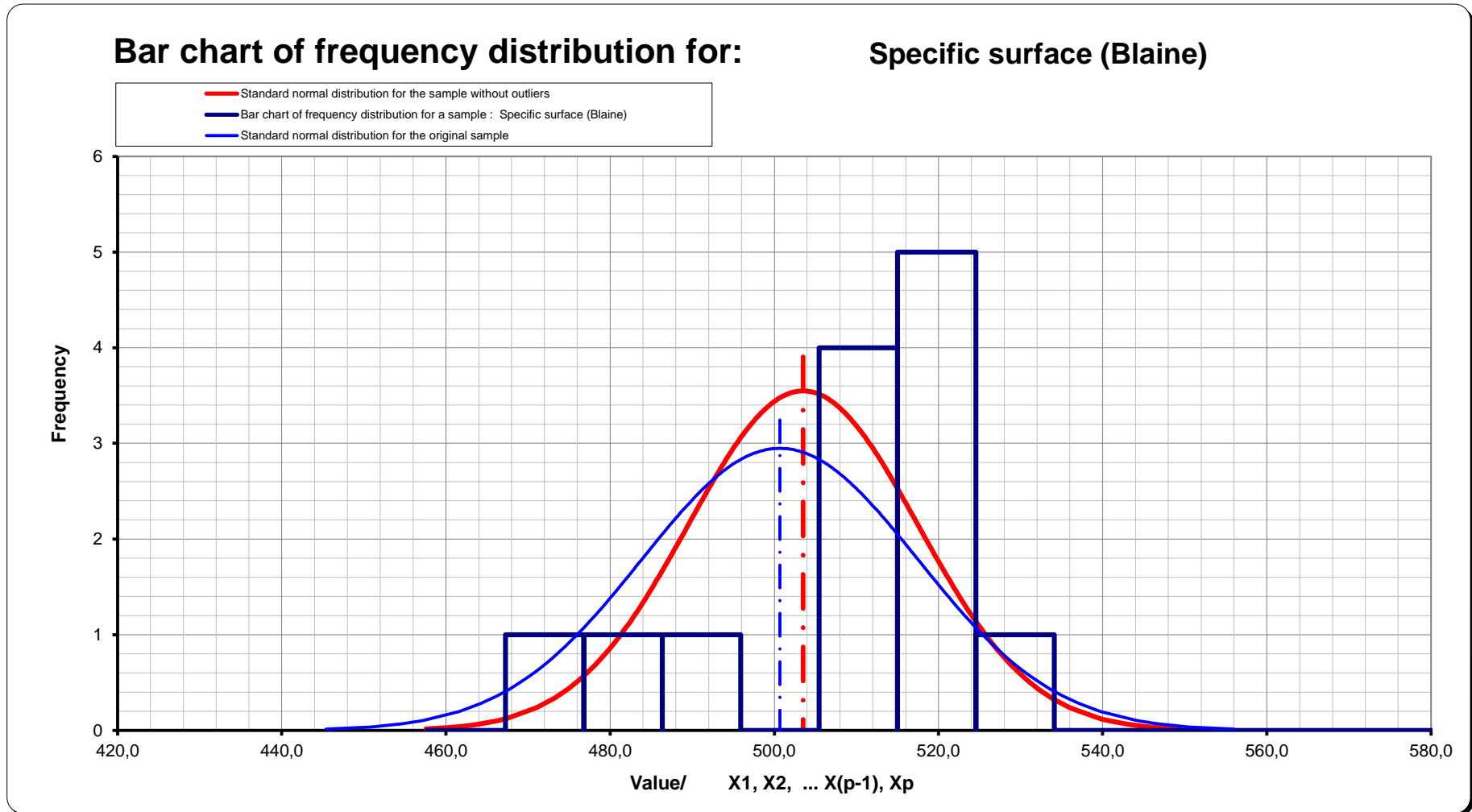
	1	Values x_1, x_2 are not outliers
	1	Values x_p, x_{p-1} are not biased values
	1	Values x_1, x_2 are not outliers
	1	Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,171
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,159
Upper critical values	$Q_{v,\alpha,5\%}$	0,361
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

	0,034	0,431	0,203	0,215
	0,192	0,198	0,054	0,046
	0,376	0,392	0,376	0,392
	1	0	1	1
	1	1	1	1



A) Summary statistics for a sample :

		Specific gravity					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	14	13	12	13	10	14
Minimum value	X _{min} = X ₁	2,87	2,88	2,91	2,87	2,87	2,87
Maximum value	X _{max} = X _p	3,05	3,05	3,05	3,03	3,02	3,05
Range of sample R = difference L _{m95%} - L _{m95%}	X _{max} - X _{min}	0,18	0,17	0,14	0,16	0,15	0,18
	$\Delta L_{95\%}$	0,258					0,258
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	2,823					2,823
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	2,852					2,852
Lower Irwin confidence limit (for P=95%)	X _{minlw1-5%}	2,801					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	2,817	2,849				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	2,832	2,861				
Average (arithmetic mean) $\bar{x} = 1/p \sum(x_i) =$		2,981	2,990	2,999	2,976	2,960	2,981
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,036	0,037	0,040	0,037	0,045	0,036
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	3,13			3,12		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	3,145			3,134		
Upper Irwin confidence limit (for P=99%)	X _{maxlw1-5%}	3,109					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	3,110					3,11
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	3,139					3,139
Standard deviation of a sample	S _{x,n-1}	0,0596	0,0523	0,0423	0,0585	0,0575	0,0596
Standard deviation	S _{x,0}	0,0574	0,0502	0,0405	0,0562	0,0546	0,0574
Coefficient of variation	v	2,0%	1,7%	1,4%	2,0%	1,9%	2,0%
Standard skewness	Sk _{est}	-0,910	-1,112	-1,201	-0,892	-0,582	-0,910
Standard kurtosis (exces)	Y ₂	-0,585	0,175	0,708	-0,774	-1,468	-0,585
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,160	2,179	2,201	2,179	2,262	2,160
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,650	2,681	2,718	2,681	2,821	2,650

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,383
	$\lambda_{calc,1,2}$	0,174
	$\lambda_{calc,n,n-1}$	0,348
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

	1,411	1,441	1,411	1,518
	0,598	0,494	0,178	0,183
	0,398	0,494	0,000	0,183
	1	1	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,862
Grubb $i=p$	G_p	1,158
Upper critical values	$G_{h,1\%}$	2,755
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.1	$G_{h,5\%}$	2,507
		1 ...
		1 ...

	2,294
	1,265
	2,699

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 1 Value x_p is not outlier

Grubb $i=1,2$	$G_{1,2}$	0,498
Grubb $i=p,p-1$	$G_{p,p-1}$	0,905
Lower critical values	$G_{d,1\%}$	0,228
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.2	$G_{d,5\%}$	0,311
		1 ...
		1 ...

	2,462
	1
	1

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

1 Value x_1 is not biased
 1 Value x_p is not biased

	0,498
	0,905
	0,202

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

	$G_{d,5\%}$	0,311
		1 ...
		1 ...

	0,284
	1
	1

Test for an afterelimination of two biased values based on a level of signifiacne of 5%

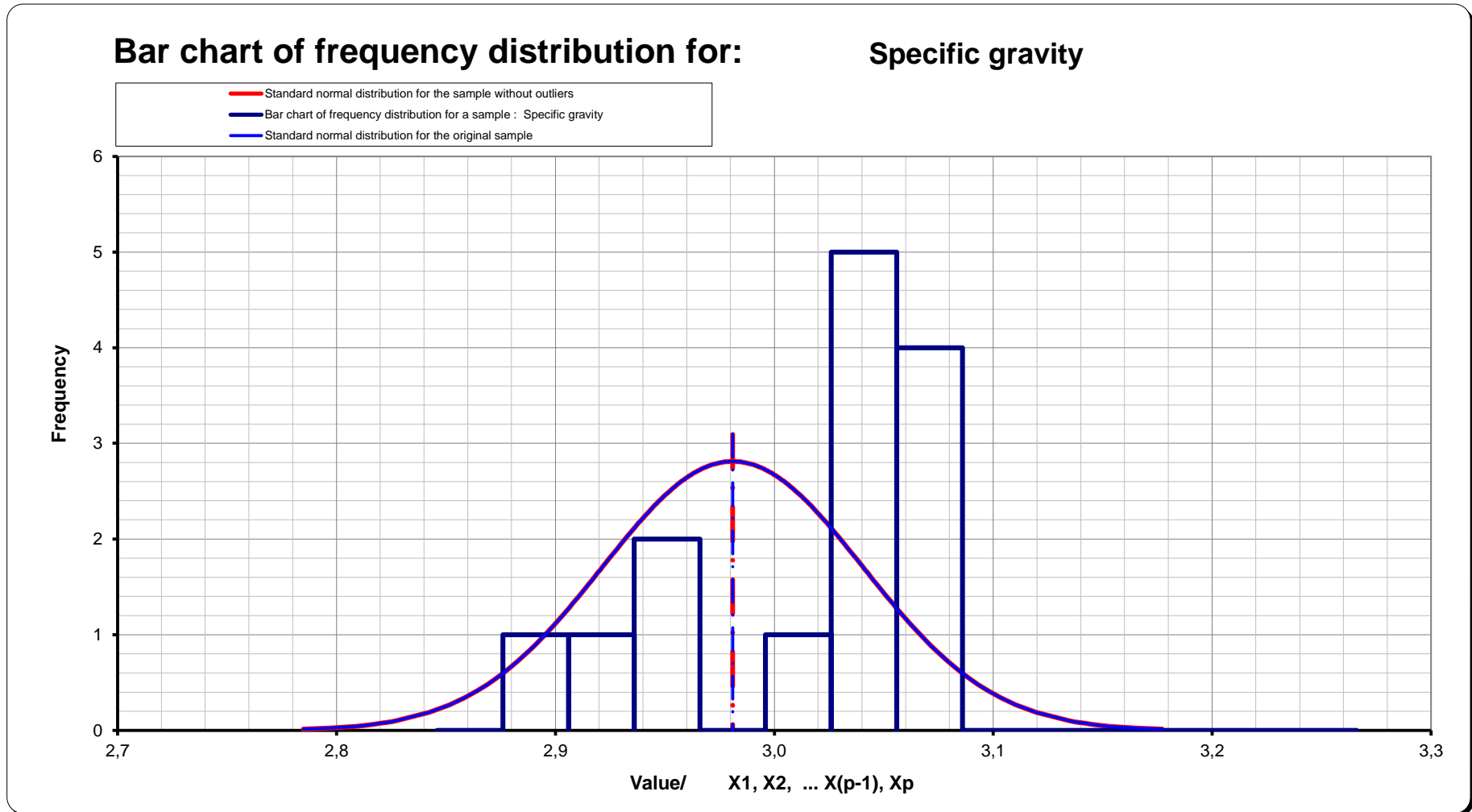
1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,056
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,111
Upper critical values	$Q_{v,\alpha,5\%}$	0,349
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

	0,176	0,143	0,062	0,067
	0,118	0,143	0,000	0,067
	0,361	0,376	0,361	0,412
	1	1	1	1
	1	1	1	1



A) Summary statistics for a sample :

		Initial setting time					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	16	14	13	15	14	15
Minimum value	X _{min} = X ₁	180	186,00	187,00	180,00	180,00	180,00
Maximum value	X _{max} = X _p	276	276,00	276,00	248,00	243,00	248,00
Range of sample R =	X _{max} - X _{min}	96	90,00	89,00	68,00	63,00	68,00
difference L _{m95%} - L _{m95%}	ΔL _{95%}	112,2					93,6
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	148,3					155,6
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	160,7					166
Lower Irwin confidence limit (for P=95%)	X _{minIw1-5%}	151,9					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	141,7	156,7				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	148,7	162,6				
Average (arithmetic mean) $\bar{x} =$	$1/p \sum(x_i) =$	216,8	222,0	224,8	212,8	210,3	212,8
Precision of a measure of the mean (for P=95%)	± ε	14,5	15,8	16,6	15,1	15,8	12,5
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	284,9			267,5		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	291,9			272,9		
Upper Irwin confidence limit (for P=99%)	X _{maxIw1-5%}	282,1					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	272,9					259,6
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	285,3					270
Standard deviation of a sample	S _{x,n-1}	26,33	23,71	22,2	21,8	20,24	21,8
Standard deviation	S _{x,0}	25,49	22,85	21,33	21,06	19,5	21,06
Coefficient of variation	v	12,1%	10,7%	9,9%	10,2%	9,6%	10,2%
Standard skewness	Sk _{est}	0,414	0,547	0,706	-0,232	-0,350	-0,232
Standard kurtosis (exces)	Y ₂	0,283	1,065	1,666	-0,928	-1,087	-0,928
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,132	2,160	2,179	2,145	2,160	2,145
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,603	2,650	2,681	2,625	2,650	2,625

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,338
	$\lambda_{calc,1,2}$	0,000
	$\lambda_{calc,n,n-1}$	1,098
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%				
	1,383	1,411	1,359	1,383
	0,044	0,516	0,000	0,000
	1,225	1,313	0,237	0,615
	1	1	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,398
Grubb $i=p$	G_p	2,248
Upper critical values	$G_{h,1\%}$	2,852
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.1	$G_{h,5\%}$	2,585
		1 ...
		1 ...
Grubb $i=1,2$	$G_{1,2}$	0,700
Grubb $i=p,p-1$	$G_{p,p-1}$	0,590
Lower critical values	$G_{d,1\%}$	0,277
for the Grubb-test		1 ...
according to ISO 5725-2,		1 ...
clause 7.3.4.2	$G_{d,5\%}$	0,360
		1 ...
		1 ...

	1,771
	2,899
	2,755
	2,507
	1
	0
	1
	0
	0,700
	0,590
	0,228
	1
	1
	1
	0,311
	1
	1

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 0 x_p^{**} is the outlier
Test for an afterelimination of one biased value based on a level of signifiacne of 5%
 1 Value x_1 is not biased
 0 x_p^* is the biased value

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

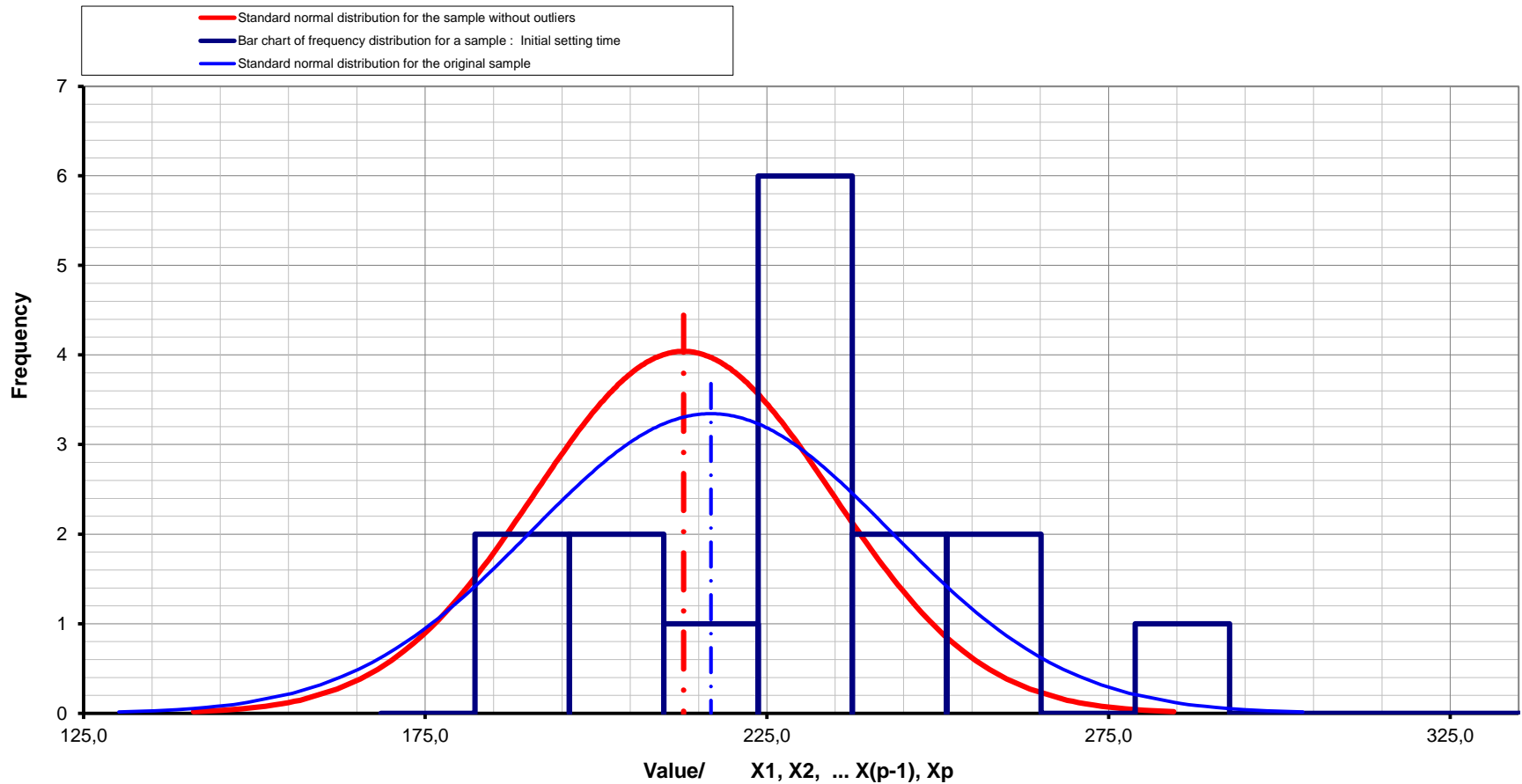
1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values
Test for an afterelimination of two biased values based on a level of signifiacne of 5%
 1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,000
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,292
Upper critical values	$Q_{v,\alpha,5\%}$	0,329
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%				
	0,011	0,124	0,000	0,000
	0,311	0,315	0,074	0,190
	0,349	0,361	0,338	0,349
	1	1	1	1
	1	1	1	1

Bar chart of frequency distribution for: Initial setting time



A) Summary statistics for a sample :

Final setting time						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 16	15	14	15	13	15
Minimum value	X _{min} = X ₁ = 250	265,00	271,00	250,00	250,00	250,00
Maximum value	X _{max} = X _p = 423	423,00	423,00	300,00	295,00	300,00
Range of sample R =	X _{max} - X _{min} = 173	158,00	152,00	50,00	45,00	50,00
difference L _{m95%} - L _{m98%}	ΔL _{95%} = 160,8					60,8
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%} = 193,2					245,3
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%} = 210,9					252,1
Lower Irwin confidence limit (for P=95%)	X _{minlw1-5%} = 216,2					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%} = 183,8	189,3				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%} = 193,8	210				
Average (arithmetic mean) $\bar{x} = 1/p \sum(x_i) =$	291,3	294,0	296,1	282,5	279,8	282,5
Precision of a measure of the mean (for P=95%)	± ε = 20,8	21,6	22,6	21,6	23,7	8,1
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%} = 388,8			314,4		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%} = 398,8			322,3		
Upper Irwin confidence limit (for P=99%)	X _{maxlw1-5%} = 348,8					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%} = 371,7					312,9
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%} = 389,4					319,7
Standard deviation of a sample	S _{x,n-1} = 37,71	37,33	37,84	14,18	13,24	14,18
Standard deviation	S _{x,0} = 36,51	36,07	36,46	13,7	12,72	13,7
Coefficient of variation	v = 12,9%	12,7%	12,8%	5,0%	4,7%	5,0%
Standard skewness	Sk _{est} = 3,095	3,305	3,305	-0,714	-0,771	-0,714
Standard kurtosis (exces)	Y ₂ = 11,323	11,973	11,716	0,286	0,615	0,286
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%} = 2,132	2,145	2,160	2,145	2,179	2,145
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%} = 2,603	2,625	2,650	2,625	2,681	2,625

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,338
	$\lambda_{calc,1,2}$	0,411
	$\lambda_{calc,n,n-1}$	3,369
Value x1 is not outlier		1 ...
xp ** is an outlier		0 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%			
1,359	1,383	1,359	1,411
0,166	0,110	1,095	1,179
3,410	3,374	0,000	0,000
1	1	1	1
0	0	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G_1	1,095
Grubb_i=p	G_p	3,492
Upper critical values	$G_{h,1\%}$	2,852
for the Grubb-test		1 ...
according to ISO 5725-2,		0 ...
clause 7.3.4.1	$G_{h,5\%}$	2,585
		1 ...
		0 ...
Grubb_i=1,2	$G_{1,2}$	1,000
Grubb_i=p,p-1	$G_{p,p-1}$	0,120
Lower critical values	$G_{d,1\%}$	0,277
for the Grubb-test		1 ...
according to ISO 5725-2,		0 ...
clause 7.3.4.2	$G_{d,5\%}$	0,360
		1 ...
		0 ...

1,179
9,908
2,806
2,249
1,000
0,120
0,253
0,337

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x1 is not outlier
 0 xp ** is the outlier
 1 Value x1 is not biased
 0 xp * is the biased value

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

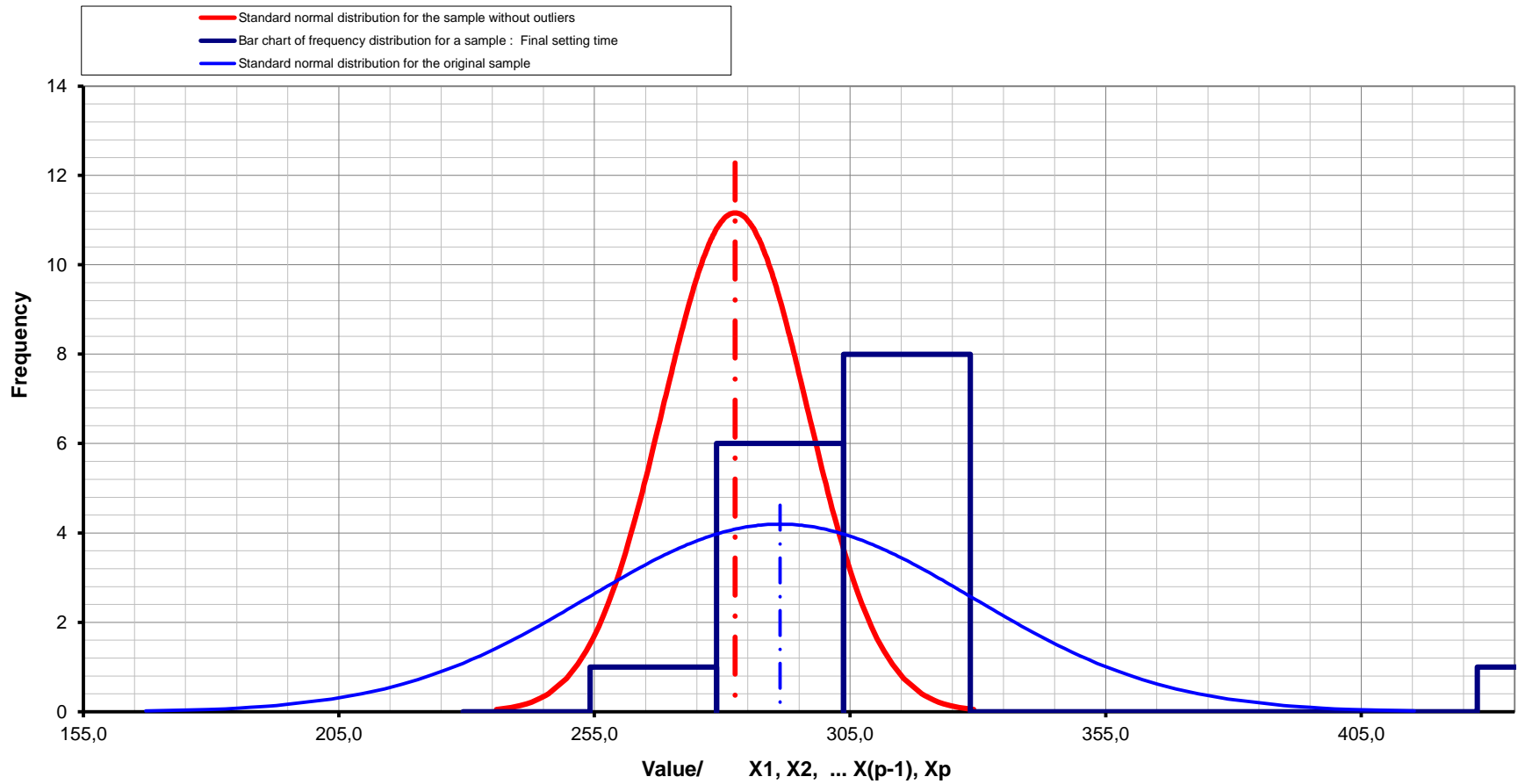
1 Values x1, x2 are not outliers
 0 xp *, xp-1 * are biased values
 1 Values x1, x2 are not outliers
 0 xp *, xp-1 * are biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... (x2-x1)	Q_1	0,087
Dixon_i=p, ... (xp-x(p-1))	Q_p	0,711
Upper critical values	$Q_{v,\alpha,5\%}$	0,329
Value x1 is not biased		1 ...
xp * is the biased value		0 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%			
0,038	0,026	0,300	0,333
0,778	0,809	0,000	0,000
0,338	0,349	0,338	0,361
1	1	1	1
0	0	1	1

Bar chart of frequency distribution for: Final setting time



A) Summary statistics for a sample :

		Water content					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	16	14	13	15	14	16
Minimum value	X _{min} = X ₁	26,9	27,20	27,40	26,90	26,90	26,90
Maximum value	X _{max} = X _p	29	29,00	29,00	28,80	28,75	29,00
Range of sample R = difference L _{m95%} - L _{m95%}	X _{max} - X _{min}	2,1	1,80	1,60	1,90	1,85	2,10
	$\Delta L_{95\%}$	2,938					2,938
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	26,09					26,093
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	26,42					26,417
Lower Irwin confidence limit (for P=95%)	X _{minlw1-5%}	26,308					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	25,921	26,336				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	26,105	26,488				
Average (arithmetic mean) $\bar{x} = 1/p \sum(x_i) =$		27,89	28,03	28,09	27,81	27,74	27,89
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,38	0,41	0,43	0,40	0,41	0,38
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	29,667			29,426		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	29,851			29,585		
Upper Irwin confidence limit (for P=99%)	X _{maxlw1-5%}	29,692					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	29,36					29,355
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	29,68					29,679
Standard deviation of a sample	S _{x,n-1}	0,689	0,614	0,589	0,644	0,605	0,689
Standard deviation	S _{x,0}	0,6672	0,5916	0,5659	0,6218	0,5828	0,6672
Coefficient of variation	v	2,5%	2,2%	2,1%	2,3%	2,2%	2,5%
Standard skewness	Sk _{est}	0,190	0,242	0,189	0,226	0,316	0,190
Standard kurtosis (exces)	Y ₂	-1,320	-1,624	-1,745	-1,276	-1,079	-1,320
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,132	2,160	2,179	2,145	2,160	2,132
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,603	2,650	2,681	2,625	2,650	2,603

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,338
	$\lambda_{calc,1,2}$	0,000
	$\lambda_{calc,n,n-1}$	0,300
Value x_1 is not outlier		1 ...
Value x_p is not outlier		1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

	1,383	1,411	1,359	1,383
	0,338	0,141	0,000	0,000
	0,338	0,353	0,080	0,343
Value x_1 is not outlier	1	1	1	1
Value x_p is not outlier	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $_i=1$	G_1	1,431
Grubb $_i=p$	G_p	1,617
Upper critical values for the Grubb-test according to ISO 5725-2, clause 7.3.4.1	$G_{h,1\%}$	2,852
	$G_{h,5\%}$	2,585
		1 ...
		1 ...

	1,836
	1,846
	2,755

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 1 Value x_p is not outlier

Grubb $_i=1,2$	$G_{1,2}$	0,719
Grubb $_i=p,p-1$	$G_{p,p-1}$	0,763
Lower critical values for the Grubb-test according to ISO 5725-2, clause 7.3.4.2	$G_{d,1\%}$	0,277
	$G_{d,5\%}$	0,360
		1 ...
		1 ...

	2,507
	1 Value x_1 is not biased
	1 Value x_p is not biased

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

1 Value x_1 is not biased
 1 Value x_p is not biased

Grubb $_i=1,2$	$G_{1,2}$	0,719
Grubb $_i=p,p-1$	$G_{p,p-1}$	0,763
Lower critical values for the Grubb-test according to ISO 5725-2, clause 7.3.4.2	$G_{d,1\%}$	0,277
	$G_{d,5\%}$	0,360
		1 ...
		1 ...

	0,719
	0,763
	0,228

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

	$G_{d,5\%}$	0,360
		1 ...
		1 ...

	0,311
	1 Value x_1, x_2 are not outliers
	1 Value x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of signifiacne of 5%

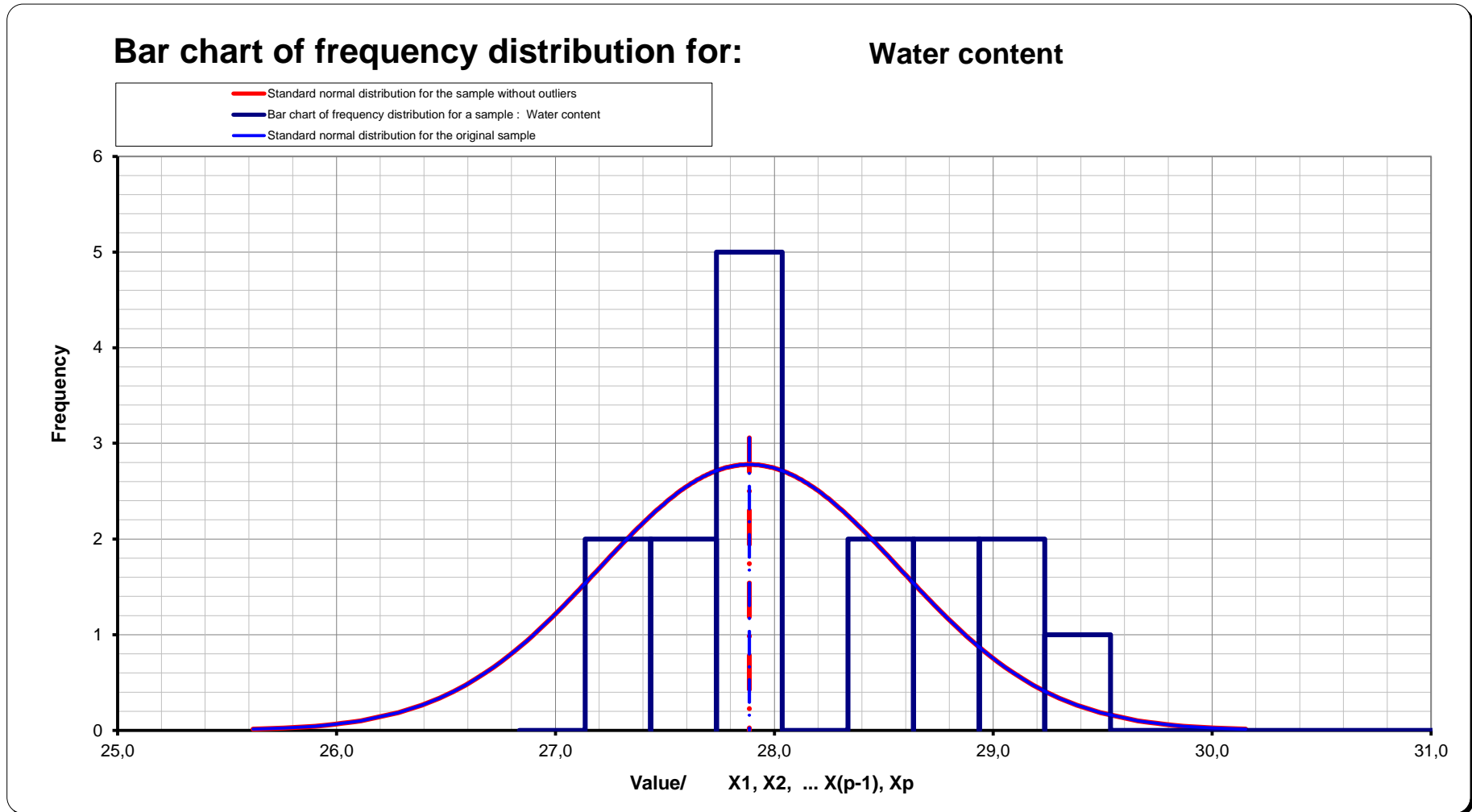
1 Value x_1, x_2 are not outliers
 1 Value x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $_i=1, \dots (x_2-x_1)$	Q_1	0,000
Dixon $_i=p, \dots (x_p-x_{p-1})$	Q_p	0,095
Upper critical values	$Q_{v,\alpha,5\%}$	0,329
Value x_1 is not biased		1 ...
Value x_p is not biased		1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

	0,111	0,050	0,000	0,000
	0,111	0,125	0,026	0,108
	0,349	0,361	0,338	0,349
Value x_1 is not biased	1	1	1	1
Value x_p is not biased	1	1	1	1



A) Summary statistics for a sample :

		Volume soundness (Le_Chatelier)					
		X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	16	11	9	14	13	14
Minimum value	X _{min} = X ₁	0	0,20	0,30	0,00	0,00	0,00
Maximum value	X _{max} = X _p	1	1,00	1,00	0,70	0,50	0,70
Range of sample R =	X _{max} - X _{min}	1	0,80	0,70	0,70	0,50	0,70
difference L _{m95%} - L _{m95%}	ΔL _{95%}	1,44					1,06
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	-0,52					-0,39
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	-0,36					-0,27
Lower Irwin confidence limit (for P=95%)	X _{minlw1-5%}	-0,24					
Lower Grubbs confidence limit (for P=99%)	X _{minG1-1%}	-0,61	-0,2				
Lower Grubbs confidence limit (for P=95%)	X _{minG1-5%}	-0,52	-0,14				
Average (arithmetic mean) $\bar{x} =$	$1/p \sum(x_i) =$	0,36	0,52	0,59	0,26	0,23	0,26
Precision of a measure of the mean (for P=95%)	± ε	0,19	0,24	0,28	0,20	0,21	0,15
Upper Grubbs confidence limit (for P=99%)	X _{maxGp-5%}	1,24			0,83		
Upper Grubbs confidence limit (for P=95%)	X _{maxGp-1%}	1,33			0,89		
Upper Irwin confidence limit (for P=99%)	X _{maxlw1-5%}	1,14					
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	1,08					0,79
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	1,24					0,91
Standard deviation of a sample	S _{x,n-1}	0,339	0,282	0,262	0,244	0,218	0,244
Standard deviation	S _{x,0}	0,328	0,269	0,247	0,235	0,209	0,235
Coefficient of variation	v	94,2%	54,2%	44,4%	93,8%	94,8%	93,8%
Standard skewness	Sk _{est}	0,691	0,786	0,799	0,263	0,165	0,263
Standard kurtosis (exces)	Y ₂	-0,365	-0,296	-0,505	-1,315	-1,756	-1,315
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,132	2,228	2,306	2,160	2,179	2,160
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,603	2,764	2,897	2,650	2,681	2,650

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\lambda_{\alpha(n)}$	1,338
	$\lambda_{calc,1,2}$	0,000
	$\lambda_{calc,n,n-1}$	0,000

Value x_1 is not outlier 1 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiacne of 5%

1,477	1,566	1,383	1,411
0,000	0,000	0,000	0,000
0,000	0,000	0,851	0,000

1 1 1 1
 1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb $i=1$	G_1	1,062
Grubb $i=p$	G_p	1,888
Upper critical values	$G_{h,1\%}$	2,852

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.1

$G_{h,5\%}$	2,585
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Grubb $i=1,2$	$G_{1,2}$	0,567
Grubb $i=p,p-1$	$G_{p,p-1}$	0,406
Lower critical values	$G_{d,1\%}$	0,277

for the Grubb-test 1 ...
 according to ISO 5725-2, 1 ...
 clause 7.3.4.2

$G_{d,5\%}$	0,360
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1,844
3,033
2,564

Test for an afterelimination of one outlier based on a level of signifiacne of 1%

1 Value x_1 is not outlier
 0 x_p^{**} is the outlier
 1 Value x_1 is not biased
 0 x_p^* is the biased value

2,355

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

0,567
0,406
0,145

Test for an afterelimination of two outliers based on a level of signifiacne of 5%

1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values
 1 Values x_1, x_2 are not outliers
 1 Values x_p, x_{p-1} are not biased values

0,221

Test for an afterelimination of two biased values based on a level of signifiacne of 5%

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon $i=1, \dots (x_2-x_1)$	Q_1	0,000
Dixon $i=p, \dots (x_p-x_{p-1})$	Q_p	0,000
Upper critical values	$Q_{v,\alpha,5\%}$	0,329

Value x_1 is not biased 1 ...
 Value x_p is not biased 1 ...

Test for an afterelimination of one biased value based on a level of signifiacne of 5%

0,000	0,000	0,000	0,000
0,000	0,000	0,286	0,000
0,392	0,437	0,349	0,361

1 1 1 1
 1 1 1 1

Bar chart of frequency distribution for:

Volume soundness (Le_Chatelier)

- Standard normal distribution for the sample without outliers
- Bar chart of frequency distribution for a sample : Volume soundness (Le_Chatelier)
- Standard normal distribution for the original sample

