

**A) Summary statistics for a sample :**

SO3 - content						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 15	14	13	14	13	14
Minimum value	$x_{min} = x_1 = 2,985$	3,17	3,18	2,99	2,99	3,17
Maximum value	$x_{max} = x_p = 3,45$	3,45	3,45	3,44	3,36	3,45
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{max} - x_{min} = 0,465$	0,28	0,27	0,46	0,38	0,28
	$\Delta L_{95\%} = 0,5034$					0,3868
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%} = 2,9647$					3,056
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%} = 3,0210$					3,0998
Lower Irwin confidence limit (for P=95%)	$x_{minlw1-5\%} = 3,0159$					
Lower Grubbs confidence limit (for P=99%)	$x_{minG1-1\%} = 2,9434$	3,0466				
Lower Grubbs confidence limit (for P=95%)	$x_{minG1-5\%} = 3,0088$	3,0688				
Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) = 3,2727$		3,2932	3,3027	3,2600	3,2462	3,2932
Precision of a measure of the mean (for P=95%)	$\pm \epsilon = 0,0673$	0,0703	0,0738	0,0703	0,0738	0,0536
Upper Grubbs confidence limit (for P=99%)	$x_{maxGp-5\%} = 3,5366$			3,5373		
Upper Grubbs confidence limit (for P=95%)	$x_{maxGp-1\%} = 3,602$			3,5648		
Upper Irwin confidence limit (for P=99%)	$x_{maxlw1-5\%} = 3,5941$					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%} = 3,5244$					3,4866
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%} = 3,5807$					3,5304
Standard deviation of a sample	$s_{x,n-1} = 0,11735$	0,0895	0,08553	0,11063	0,10174	0,0895
Standard deviation	$s_{x,0} = 0,11337$	0,08624	0,08217	0,1066	0,09775	0,08624
Coefficient of variation	$v = 3,6\%$	2,7%	2,6%	3,4%	3,1%	2,7%
Standard skewness	$S_k_{est} = -0,700$	0,443	0,456	-0,877	-1,297	0,443
Standard kurtosis (exces)	$\gamma_2 = 1,433$	-0,840	-0,872	2,014	2,770	-0,840
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%} = 2,145$	2,160	2,179	2,160	2,179	2,160
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%} = 2,625$	2,650	2,681	2,650	2,681	2,650

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)

$\lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	1,632
$\lambda_{\text{calc},n,n-1}$	0,088

$x_1^{**}$       0 ...  
 Value  $x_p$  is not outlier      1 ...

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

1,383	1,411	1,383	1,411
0,116	0,487	1,735	1,893
0,116	0,122	0,750	0,051

1      1      0      0  
 1      1      1      1

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb\_i=1

$G_1$	2,452
$G_p$	1,511

Upper critical values

$G_{h,1\%}$	2,806
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for the Grubb-test

	1 ...
	1 ...

according to ISO 5725-2,

clause 7.3.4.1	$G_{h,5\%}$	2,249
	0 ...	0 ...
	1 ...	1 ...

Lower critical values

$G_{1,2}$	0,525
$G_{p,p-1}$	0,743

for the Grubb-test

	1 ...
	1 ...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1 ...	1 ...
	1 ...	1 ...

Upper critical values

$G_{d,1\%}$	0,253
$G_{d,p-1}$	0,228

for the Grubb-test

	1 ...
	1 ...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1 ...	1 ...
	1 ...	1 ...

for the Grubb-test

	1 ...
	1 ...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1 ...	1 ...
	1 ...	1 ...

Test for an afterelimination of one outlier based on a level of signifiance of 1%

$x_1^{**}$  is the outlier

Value  $x_p$  is not outlier

Test for an afterelimination of one biased value based on a level of signifiance of 5%

$x_1^*$  is the biased value

Value  $x_p$  is not biased

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values  $x_1, x_2$  are not outliers

Values  $x_p, x_{p-1}$  are not biased values

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values  $x_1, x_2$  are not outliers

Values  $x_p, x_{p-1}$  are not biased values

**B3) Tests by Dixon for an afterelimination of outliers or biased values**

Dixon\_i=1, ... ( $x_2 - x_1$ )

$Q_1$	0,398
$Q_p$	0,022

Upper critical values

$Q_{v,a,5\%}$	0,338
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$x_1^*$  is the biased value

	0 ...
	1 ...

Value  $x_p$  is not biased

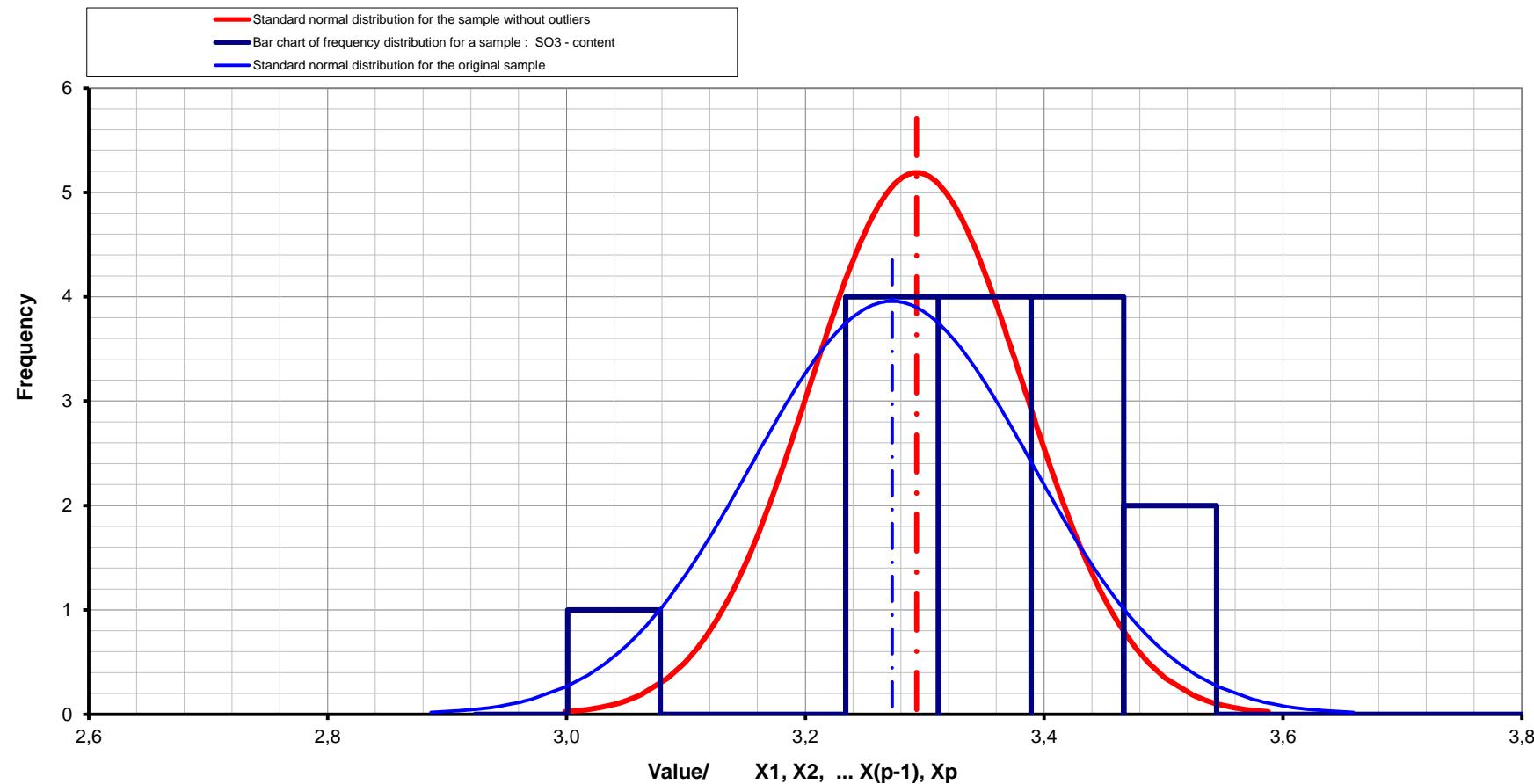
	1 ...
	1 ...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,036	0,148	0,407	0,493
0,036	0,037	0,176	0,013

0,349	0,361	0,349	0,361
1	1	1	1

## Bar chart of frequency distribution for: SO3 - content



**A) Summary statistics for a sample :**

CI - content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	15				14
Minimum value	$x_{min} = x_1$	0,067	0,08	0,08	0,07	0,08
Maximum value	$x_{max} = x_p$	0,094	0,09	0,09	0,09	0,09
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{max} - x_{min}$	0,027	0,02	0,02	0,03	0,02
	$\Delta L_{95\%}$	0,028				0,0224
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	0,0650				0,0694
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,0681				0,0720
Lower Irwin confidence limit (for P=95%)	$x_{min}l_{w1-5\%}$	0,0684				
Lower Grubbs confidence limit (for P=99%)	$x_{min}G_{1-1\%}$	0,0638	0,0689			
Lower Grubbs confidence limit (for P=95%)	$x_{min}G_{1-5\%}$	0,0674	0,0702			
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n}$	= 0,0821	0,0832	0,0843	0,0813	0,0805	0,0832
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0037	0,0039	0,0043	0,0039	0,0041
Upper Grubbs confidence limit (for P=99%)	$x_{max}G_{p-5\%}$	0,0968			0,096	
Upper Grubbs confidence limit (for P=95%)	$x_{max}G_{p-1\%}$	0,1004			0,0974	
Upper Irwin confidence limit (for P=99%)	$x_{max}l_{w1-5\%}$	0,1006				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	0,0961				0,0944
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	0,0992				0,097
Standard deviation of a sample	$s_{x,n-1}$	0,00652				
Standard deviation	$s_{x,0}$	0,0063	0,00519	0,00486	0,00585	0,00517
Coefficient of variation	v	7,9%	6,2%	5,8%	7,2%	6,4%
Standard skewness	$Sk_{est}$	-0,257	0,927	1,046	-0,627	-1,298
Standard kurtosis (exces)	$\gamma_2$	1,374	0,130	-0,001	2,247	3,333
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,145	2,160	2,201	2,160	2,179
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$	2,625	2,650	2,718	2,650	2,681
						2,160

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	1,587
$\lambda_{\text{calc},n,n-1}$	0,317

$x_1^{**}$       0 ...  
 Value  $x_p$  is not outlier      1 ...

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

1,383	1,441	1,383	1,411
0,000	0,215	1,773	2,012
0,400	0,429	0,709	0,402

1	1	0	0
1	1	1	1

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb\_i=1

$G_1$	2,316
$G_p$	1,825

Upper critical values

$G_{h,1\%}$	2,806
for the Grubb-test	1 ...

according to ISO 5725-2,

clause 7.3.4.1

$G_{h,5\%}$	2,249
0 ...	0 .....
1 ...	1 .....

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.1

$G_{1,2}$	0,547
$G_{p,p-1}$	0,622
$G_{d,1\%}$	0,253

Lower critical values

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.2

$G_{d,5\%}$	0,337
1 ...	1 .....
1 ...	1 .....

**Test for an afterelimination of one outlier based on a level of signifiance of 1%**

$x_1^{**}$  is the outlier

Value  $x_p$  is not outlier

3,121	2,755
2,171	2,507
0 .....	0 .....

1 .....	1 .....
1 .....	1 .....
Values $x_1, x_2$ are not outliers	Values $x_p, x_{p-1}$ are not biased values

0,547	0,228
0,622	0,311
1 .....	1 .....

0,253	0,311
1 .....	1 .....
1 .....	1 .....
Values $x_1, x_2$ are not outliers	Values $x_p, x_{p-1}$ are not biased values

**B3) Tests by Dixon for an afterelimination of outliers or biased values**

Dixon\_i=1, ... ( $x_2 - x_1$ )

$Q_1$	0,370
$Q_p$	0,074

Upper critical values

$Q_{v,a,5\%}$	0,338
$x_1^*$ is the biased value	0 ...

$x_1^*$  is the biased value

0 ...	0 .....
1 ...	1 .....

Value  $x_p$  is not biased

1 ...	1 .....
1 ...	1 .....

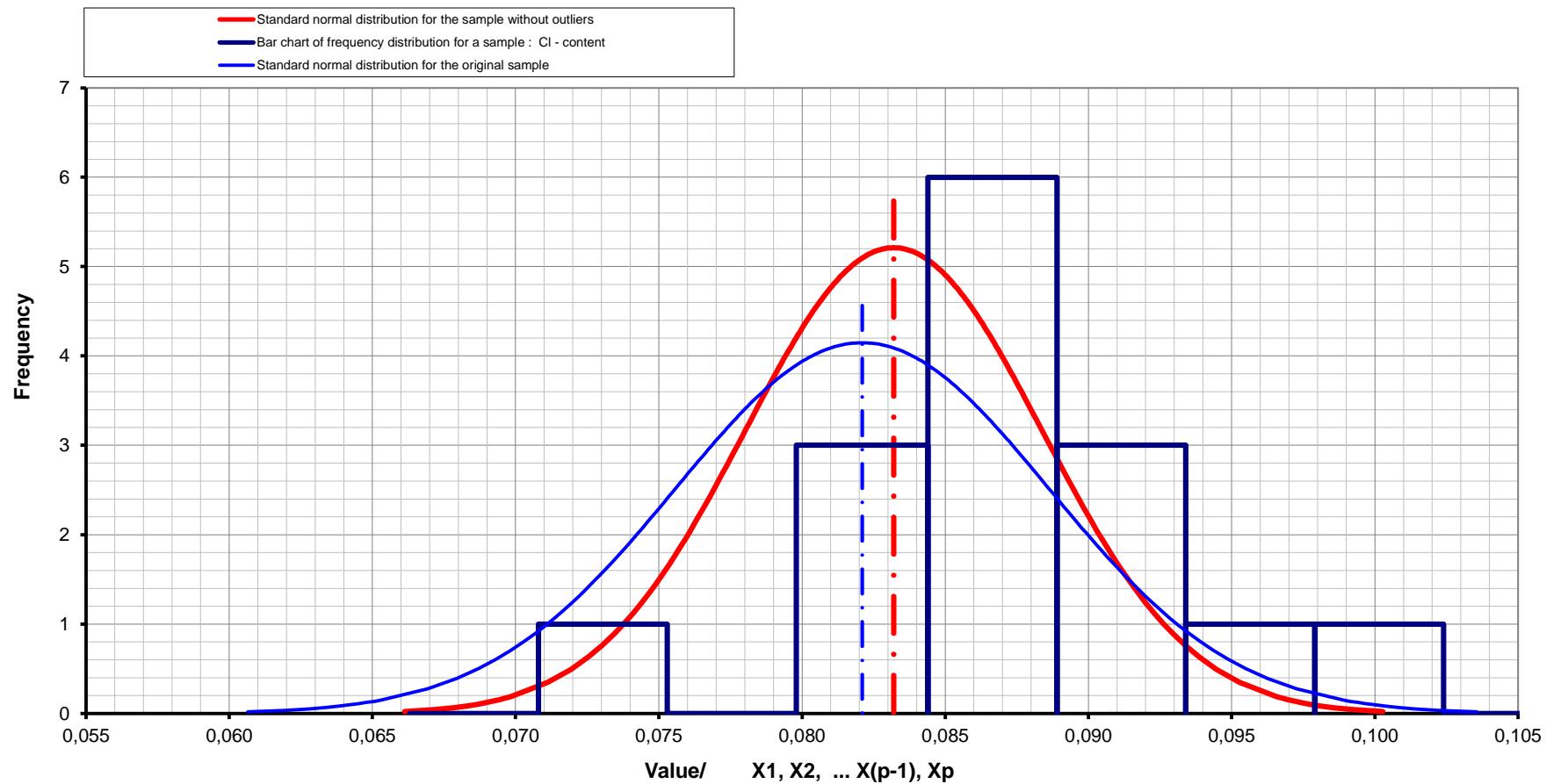
**Test for an afterelimination of one biased value based on a level of signifiance of 5%**

0,000	0,067	0,400	0,476
0,118	0,133	0,160	0,095
0,349	0,376	0,349	0,361

1	1	0	0
1	1	1	1
1	1	1	1

## Bar chart of frequency distribution for:

CI - content



**A) Summary statistics for a sample :**

Loss on Ignition						
Count (Sample size)	X <sub>1</sub> , X <sub>2</sub> , ... X(p-1), X <sub>p</sub>	X <sub>2</sub> , X <sub>3</sub> , ... X(p-1), X <sub>p</sub>	X <sub>3</sub> , X <sub>4</sub> ... X(p-1), X <sub>p</sub>	X <sub>1</sub> , X <sub>2</sub> , ... X(p-2), X(p-1)	X <sub>1</sub> , X <sub>2</sub> , ... X(p-3), X(p-2)	Sample without outliers
n	15	13	12	14	13	14
Minimum value	X <sub>min</sub> = X <sub>1</sub>	7,615	7,63	7,65	7,62	7,62
Maximum value	X <sub>max</sub> = X <sub>p</sub>	8,52	8,52	8,52	7,97	7,97
Range of sample R = difference L <sub>m95%</sub> - L <sub>M95%</sub> .....	X <sub>max</sub> - X <sub>min</sub>	0,905	0,90	0,87	0,36	0,27
	ΔL <sub>95%</sub>	0,982				0,466
Lower confidence limits after elimination of outliers (for P=98%)	L <sub>m98%</sub>	7,1819				7,4442
Lower confidence limits after elimination of outliers (for P=95%)	L <sub>m95%</sub>	7,2917				7,497
	Lower Irwin confidence limit (for P=95%)	7,3244				
	X <sub>min</sub> lw1-5%	7,1403				
	Lower Grubbs confidence limit (for P=99%)	7,2678				
Precision of a measure of the mean (for P=95%)	Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	7,7827	7,8085	7,8238	7,7300	7,7300
	± ε	0,1312	0,1440	0,1519	0,1372	0,1440
	Upper Grubbs confidence limit (for P=99%)	8,2976			7,9955	
	Upper Grubbs confidence limit (for P=95%)	8,4251			8,0211	
	Upper Irwin confidence limit (for P=99%)	8,2706				
Upper confidence limits after elimination of outliers (for P=95%)	L <sub>M95%</sub>	8,2737				7,963
Upper confidence limits after elimination of outliers (for P=98%)	L <sub>M98%</sub>	8,3835				8,0158
Standard deviation of a sample	S <sub>x,n-1</sub>	0,22893	0,23608	0,23976	0,10785	0,0862
Standard deviation	S <sub>x,0</sub>	0,22116	0,22682	0,22956	0,10392	0,08282
Coefficient of variation	V	2,9%	3,0%	3,1%	1,4%	1,1%
Standard skewness	S <sub>k<sub>est</sub></sub>	2,668	2,588	2,556	0,959	0,707
Standard kurtosis (exces)	γ <sub>2</sub>	8,232	7,613	7,326	0,290	-0,422
t-value of the Student's distribution for P=95%	t <sub>(n-1),α=2,5%</sub>	2,145	2,179	2,201	2,160	2,179
t-value of the Student's distribution for P=98%	t <sub>(n-1),α=1,0%</sub>	2,625	2,681	2,718	2,650	2,681
						2,160

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	0,000
$\lambda_{\text{calc},n,n-1}$	2,487

Value  $x_1$  is not outlier      1 ...  
 $x_p$  \*\* is an outlier      0 ...

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

1,411	1,441	1,383	1,411
0,110	0,022	0,000	0,000
2,425	2,396	0,818	0,664

1      1      1      1  
 0      0      1      1

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb\_i=1

$G_1$	0,733
$G_p$	3,221

Upper critical values

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.1

Lower critical values

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.2

$G_{h,1\%}$	2,806
$G_{h,5\%}$	2,249
$G_{d,1\%}$	0,253

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,253

$G_{d,5\%}$	0,337
$G_{d,1\%}$	0,202
$G_{d,5\%}$	0,284

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.2

$G_{d,1\%}$	0,202
$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
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$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
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$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
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$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
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$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

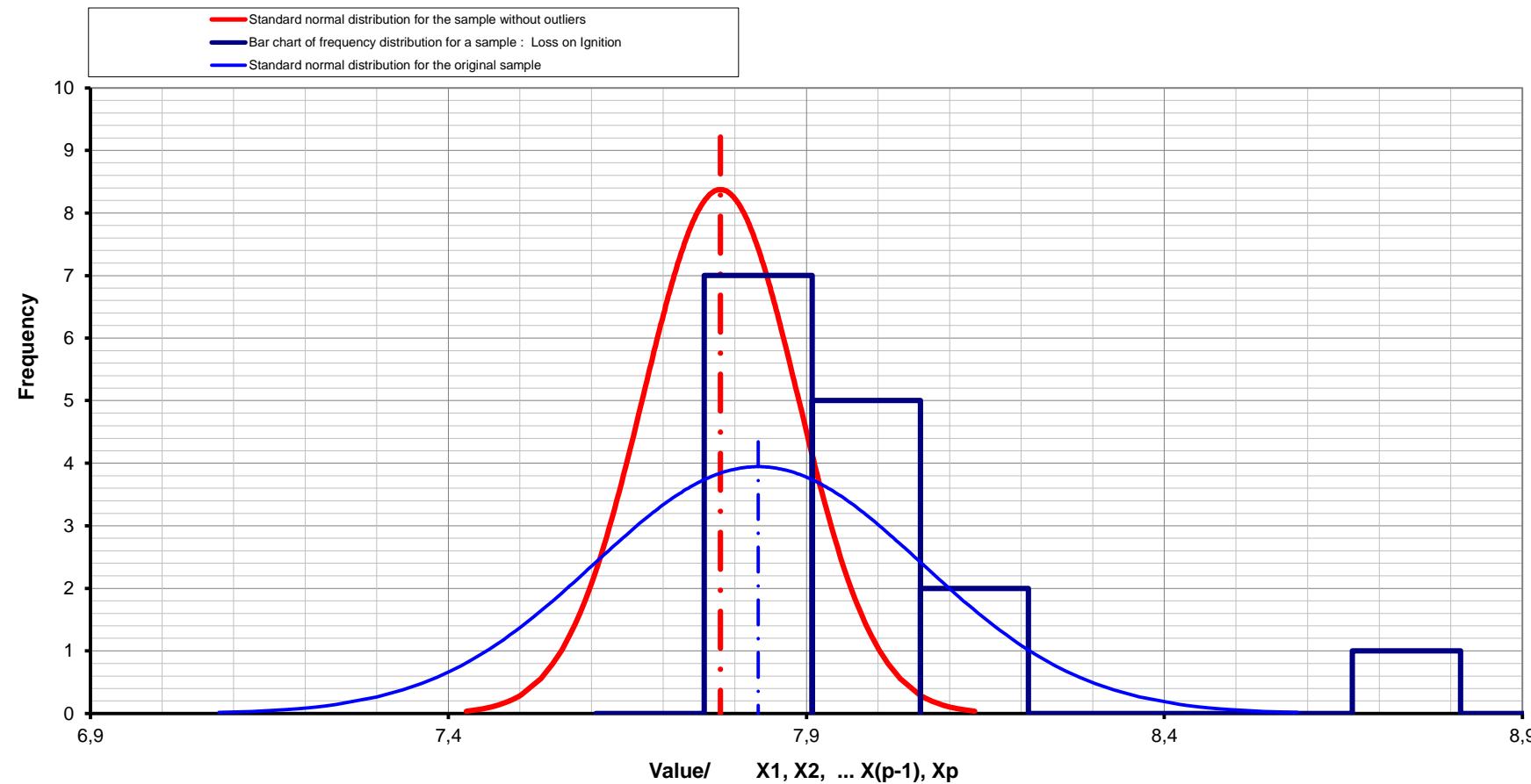
$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$	0,202

$G_{d,5\%}$	0,284
$G_{d,1\%}$	0,284
$G_{d,5\%}$	0,284

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140
$G_{d,1\%}$ </	

## Bar chart of frequency distribution for:

## Loss on Ignition



**A) Summary statistics for a sample :**

Insoluble residue						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 14	13	12	13	12	14
Minimum value	$x_{min} = x_1$ 1,47	1,50	1,52	1,47	1,47	1,47
Maximum value	$x_{max} = x_p$ 1,785	1,79	1,79	1,78	1,76	1,79
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{max} - x_{min}$ 0,315	0,29	0,27	0,31	0,29	0,32
	$\Delta L_{95\%}$ 0,4522					0,4522
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$ 1,3672					1,3672
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$ 1,4185					1,4185
Lower Irwin confidence limit (for P=95%)	$x_{minlw1-5\%}$ 1,3555					
Lower Grubbs confidence limit (for P=99%)	$x_{minG1-1\%}$ 1,3563	1,4002				
Lower Grubbs confidence limit (for P=95%)	$x_{minG1-5\%}$ 1,3822	1,4229				
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	1,6446	1,6581	1,6717	1,6338	1,6217	1,6446
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$ 0,0627	0,0658	0,0694	0,0658	0,0694	0,0627
Upper Grubbs confidence limit (for P=99%)	$x_{maxGp-5\%}$ 1,907					
Upper Grubbs confidence limit (for P=95%)	$x_{maxGp-1\%}$ 1,9329					
Upper Irwin confidence limit (for P=99%)	$x_{maxlw1-5\%}$ 1,9195					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$ 1,8707					1,8707
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$ 1,9220					1,922
Standard deviation of a sample	$s_{x,n-1}$ 0,10465					
Standard deviation	$s_{x,0}$ 0,10084	0,09554	0,08566	0,10048	0,0944	0,10465
Coefficient of variation	v 6,4%	0,09179	0,08201	0,09654	0,09038	0,10084
Standard skewness	$Sk_{est}$ -0,323	5,8%	5,1%	6,2%	5,8%	6,4%
Standard kurtosis (exces)	$\gamma_2$ -1,067	-0,366	-0,386	-0,286	-0,320	-0,323
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$ 2,160	-0,875	-0,616	-1,061	-1,146	-1,067
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$ 2,650	2,179	2,201	2,179	2,201	2,160
		2,681	2,718	2,681	2,718	2,650

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,383
	$\lambda_{\text{calc},1,2}$	0,248
	$\lambda_{\text{calc},n,n-1}$	0,050
Value $x_1$ is not outlier	1 ...	
Value $x_p$ is not outlier	1 ...	

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

1,411	1,441	1,411	1,441
0,272	0,305	0,259	0,277
0,054	0,061	0,207	0,498

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb_i=1	$G_1$	1,668	1,969
Grubb_i=p	$G_p$	1,342	1,505
Upper critical values	$G_{h,1\%}$	2,755	2,699
for the Grubb-test		1 ...	1 .....
according to ISO 5725-2,		1 ...	1 .....
clause 7.3.4.1	$G_{h,5\%}$	2,507	2,462
		1 ...	1 .....
		1 ...	1 .....

Test for an afterelimination of one outlier based on a level of signifiance of 1%

Value  $x_1$  is not outlier

Value  $x_p$  is not outlier

Grubb_i=1,2	$G_{1,2}$	0,661	0,661
Grubb_i=p,p-1	$G_{p,p-1}$	0,803	0,803
Lower critical values	$G_{d,1\%}$	0,228	0,202
for the Grubb-test		1 ...	1 .....
according to ISO 5725-2,		1 ...	1 .....
clause 7.3.4.2	$G_{d,5\%}$	0,311	0,284
		1 ...	1 .....
		1 ...	1 .....

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values  $x_1, x_2$  are not outliers

Values  $x_p, x_{p-1}$  are not biased values

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values  $x_1, x_2$  are not outliers

Values  $x_p, x_{p-1}$  are not biased values

**B3) Tests by Dixon for an afterelimination of outliers or biased values**

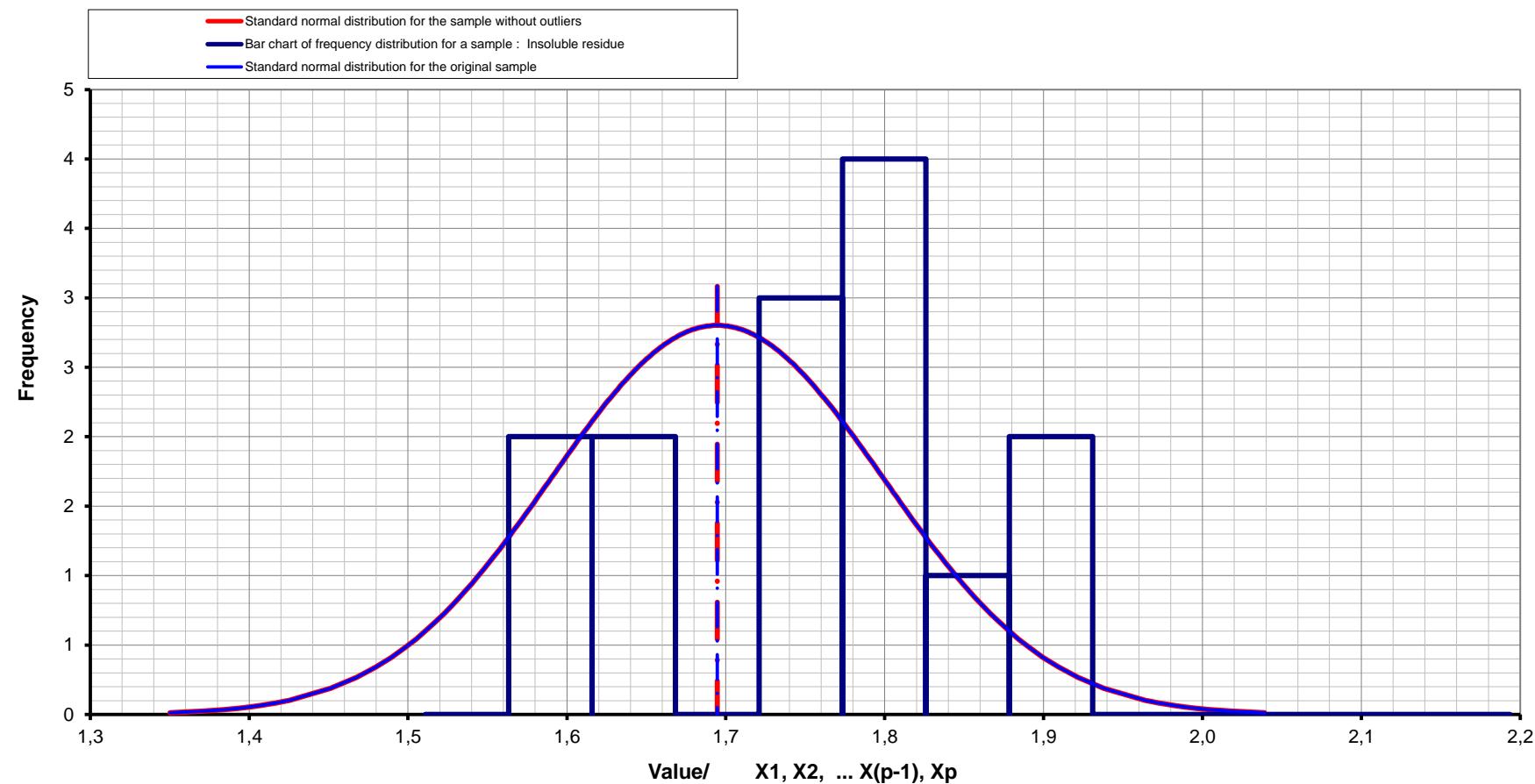
Dixon_i=1, ... ( $x_2-x_1$ )	$Q_1$	0,079	0,086
Dixon_i=p, ... ( $x_p-x_{(p-1)}$ )	$Q_p$	0,016	0,017
Upper critical values	$Q_{v,a,5\%}$	0,349	0,361
Value $x_1$ is not biased		1 ...	1 ...
Value $x_p$ is not biased		1 ...	1 ...

**Test for an afterelimination of one biased value based on a level of signifiance of 5%**

0,086	0,094	0,081	0,086
0,017	0,019	0,065	0,155
0,361	0,376	0,361	0,376

## Bar chart of frequency distribution for:

**Insoluble residue**



**A) Summary statistics for a sample :**

Natriumoxid-content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	13				
Minimum value	$x_{min} = x_1$	0,21				
Maximum value	$x_{max} = x_p$	0,72				
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{max} - x_{min}$	0,51				
	$\Delta L_{95\%}$	0,5996				
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	-0,0566				
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,0125				
	$x_{minlw1-5\%}$	0,0285				
	$x_{minG1-1\%}$	-0,059				
	$x_{minG1-5\%}$	-0,0264				
Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	0,3123					
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0865				
	$x_{maxGp-5\%}$	0,651				
	$x_{maxGp-1\%}$	0,6836				
	$x_{maxlw1-5\%}$	0,6415				
Upper confidence limits after elimination of outliers (for P=99%)	$L_{M95\%}$	0,6121				
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	0,6812				
Standard deviation of a sample	$s_{x,n-1}$	0,13758				
Standard deviation	$s_{x,0}$	0,13218				
Coefficient of variation	v	44,1%				
		43,7%	43,2%	23,5%	13,8%	13,8%
Standard skewness	$Sk_{est}$	2,546	2,495	2,447	1,877	-0,058
Standard kurtosis (exces)	$\gamma_2$	6,978	6,608	6,235	4,783	-1,106
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,179	2,201	2,228	2,201	2,228
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,681	2,718	2,764	2,718	2,764

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,411
	$\lambda_{\text{calc},1,2}$	0,038
	$\lambda_{\text{calc},n,n-1}$	2,005
Value $x_1$ is not outlier	1 ...	
$x_p$ ** is an outlier	0 ...	

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

	1,441	1,477	1,441	1,477
	0,082	0,132	0,080	0,145
	1,976	1,948	2,155	0,581
1	1	1	1	1
0	0	0	0	1

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb_i=1	G <sub>i</sub>	0,744
Grubb_i=p	G <sub>p</sub>	2,963
Upper critical values	G <sub>h,1%</sub>	2,699
for the Grubb-test	1 ...	
according to ISO 5725-2,	0 ...	
clause 7.3.4.1	G <sub>h,5%</sub>	2,462
1 ...		
0 ...		

0,791	Test for an afterelimination of one outlier based on a level of signifiance of 1%
6,752	
2,636	Test for an afterelimination of one biased value based on a level of signifiance of 5%
1 .....	Value x <sub>1</sub> is not outlier
0 .....	x <sub>p</sub> ** is the outlier
2,412	Value x <sub>1</sub> is not biased
1 .....	x <sub>p</sub> * is the biased value
0 .....	

Grubb_i=1,2	G <sub>1,2</sub>	1,059
Grubb_i=p,p-1	G <sub>p,p-1</sub>	0,068
Lower critical values	G <sub>d,1%</sub>	0,202
for the Grubb-test	1 ...	
according to ISO 5725-2,	0 ...	
clause 7.3.4.2	G <sub>d,5%</sub>	0,284
1 ...		
0 ...		

1,059	Test for an afterelimination of two outliers based on a level of signifiance of 5%
0,068	
0,174	Test for an afterelimination of two biased values based on a level of signifiance of 5%
1 .....	Values x <sub>1</sub> , x <sub>2</sub> are not outliers
0 .....	x <sub>p</sub> *, x <sub>p-1</sub> * are biased values
0,254	Test for an afterelimination of two biased values based on a level of signifiance of 5%
1 .....	Values x <sub>1</sub> , x <sub>2</sub> are not outliers
0 .....	x <sub>p</sub> *, x <sub>p-1</sub> * are biased values

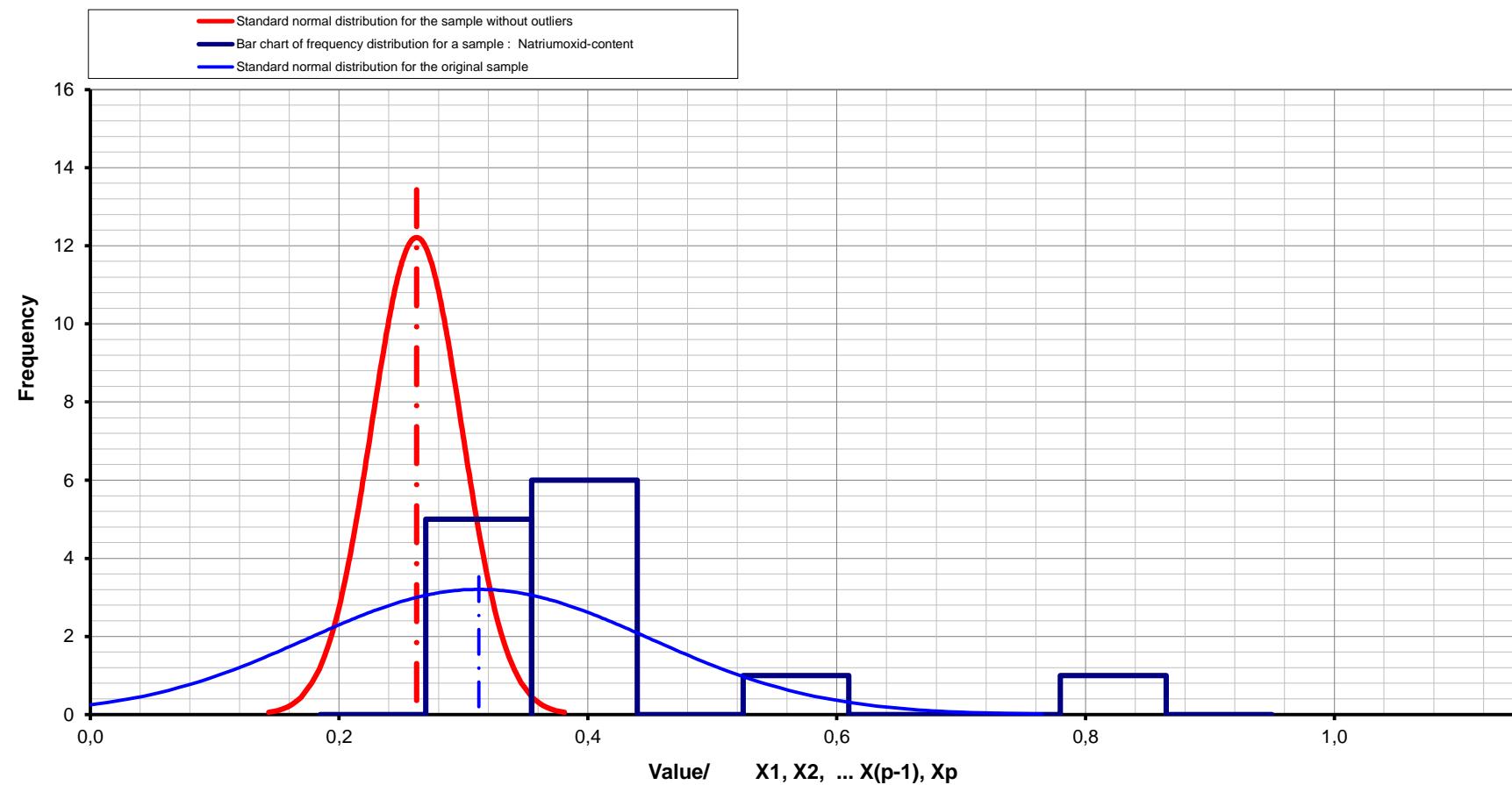
**B3) Tests by Dixon for an afterelimination of outliers or biased values**

Dixon_i=1, ... (x <sub>2</sub> -x <sub>1</sub> )	Q <sub>i</sub>	0,010
Dixon_i=p, ... (x <sub>p</sub> -x <sub>(p-1)</sub> )	Q <sub>p</sub>	0,520
Upper critical values	Q <sub>v,a,5%</sub>	0,361
Value x <sub>1</sub> is not biased	1 ...	
x <sub>p</sub> * is the biased value	0 ...	

Test for an afterelimination of one biased value based on a level of signifiance of 5%				
0,022	0,036	0,020	0,045	
0,525	0,536	0,551	0,182	
0,376	0,392	0,376	0,392	
1	1	1	1	
0	0	0	0	1

### Bar chart of frequency distribution for:

### Natriumoxid-content



**A) Summary statistics for a sample :**

Potassiumoxid-content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
n	13					11
Minimum value	$x_{\min} = x_1$	0,22				0,67
Maximum value	$x_{\max} = x_p$	0,765				0,77
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{\max} - x_{\min}$	0,545				0,10
	$\Delta L_{95\%}$	0,63				0,1358
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	0,2872				0,6399
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,3598				0,6563
	$x_{\min} l_{w1-5\%}$	0,3901				
Lower Irwin confidence limit (for P=95%)	$x_{\min} G_{1-1\%}$	0,2846				
Lower Grubbs confidence limit (for P=99%)	$x_{\min} G_{1-5\%}$	0,3188				
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	0,6748					0,7242
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0909				0,0215
Upper Grubbs confidence limit (for P=99%)	$x_{\max} G_{p-5\%}$	1,0308				
Upper Grubbs confidence limit (for P=95%)	$x_{\max} G_{p-1\%}$	1,065				
Upper Irwin confidence limit (for P=99%)	$x_{\max} l_{w1-5\%}$	0,9469				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	0,9898				0,7921
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	1,0624				0,8085
Standard deviation of a sample	$s_{x,n-1}$	0,14458				
Standard deviation	$s_{x,0}$	0,13891				
Coefficient of variation	v	21,4%				
Standard skewness	$S_k_{est}$	-3,006				
Standard kurtosis (exces)	$\gamma_2$	9,647				
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,179				
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$	2,681				
			2,201	2,228	2,201	2,228
			2,718	2,764	2,718	2,764

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)

$\lambda_{\alpha(n)}$	1,411
$\lambda_{\text{calc},1,2}$	2,635
$\lambda_{\text{calc},n,n-1}$	0,101

$x_1^{**}$   
Value  $x_p$  is not outlier

**Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%**

1,441	1,477	1,441	1,477
1,672	0,516	2,577	2,507
0,296	0,482	0,042	0,000

0 ... 1 ... 0 ... 0 ...  
1 ... 1 ... 1 ... 1 ...

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb\_i=1

$G_1$	3,146
$G_p$	0,624

Upper critical values

for the Grubb-test

according to ISO 5725-2,  
clause 7.3.4.1

$G_{h,1\%}$

0 ...

1 ...

$G_{h,5\%}$

0 ...

1 ...

Grubb\_i=1,2

Grubb\_i=p,p-1

Lower critical values

for the Grubb-test

according to ISO 5725-2,  
clause 7.3.4.2

$G_{d,1\%}$

0 ...

1 ...

$G_{d,5\%}$

0 ...

1 ...

9,982
0,659

2,636
2,412

Test for an afterelimination of one outlier based on a level of signifiance of 1%

$x_1^{**}$  is the outlier

Value  $x_p$  is not outlier

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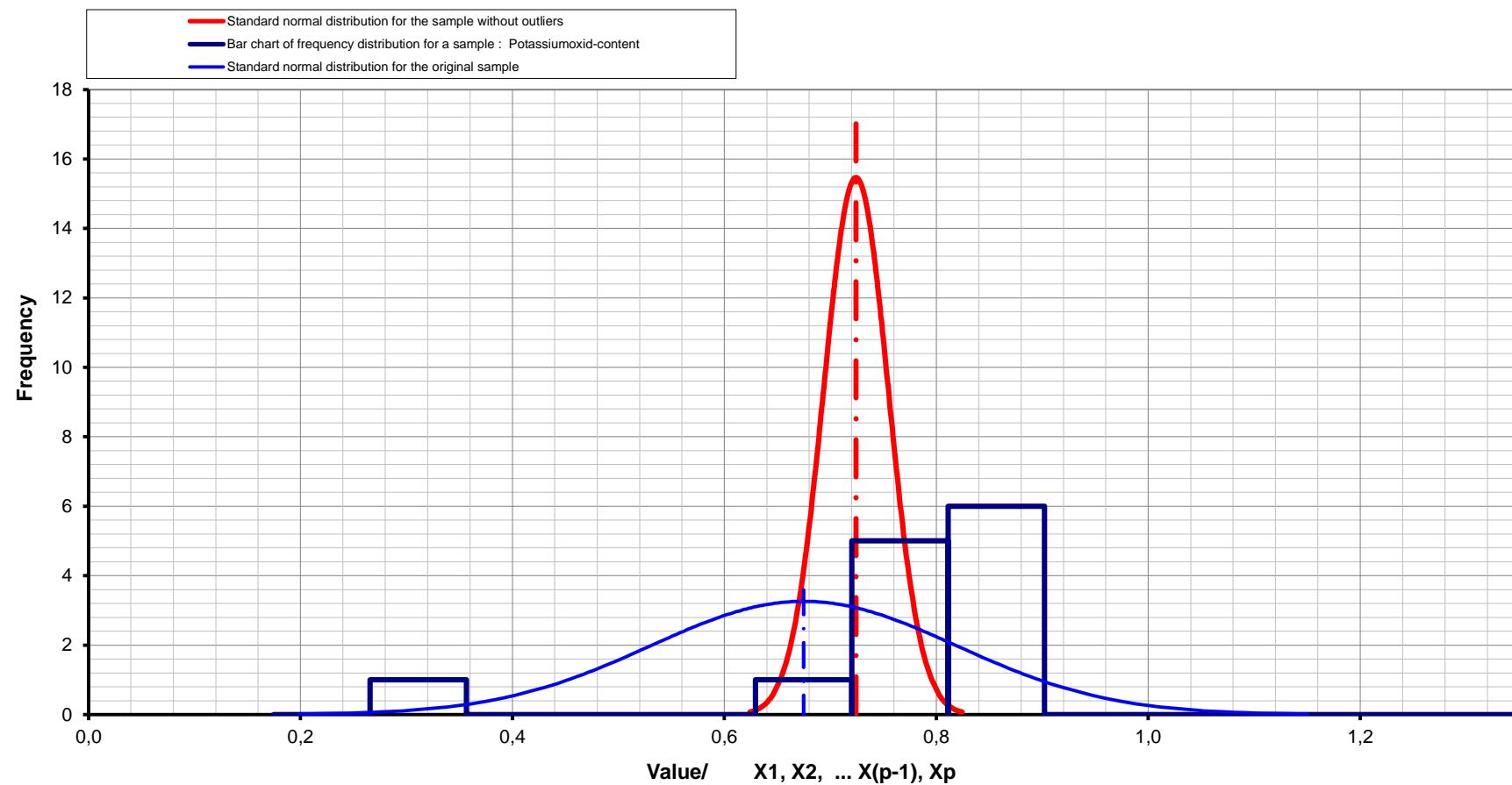
0 ...
1 ...

0 ...
1 ...

0 ...
1 ...

## Bar chart of frequency distribution for:

## Potassiumoxid-content



**A) Summary statistics for a sample :**

Slag-content - microscopically						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
n	5	4	3	4	3	3
Minimum value	$x_{min} = x_1$	11,65	17,65	11,65	11,65	15,55
Maximum value	$x_{max} = x_p$	23,5	23,50	22,35	17,65	22,35
Range of sample R = difference $L_{m95\%} - L_{M95\%}$ .....	$x_{max} - x_{min}$	11,85	7,95	5,85	10,70	6,00
	$\Delta L_{95\%}$	27,136				#HODNOTA!
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	-0,170				#HODNOTA!
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	4,572				#HODNOTA!
Lower Irwin confidence limit (for P=95%)	$x_{minlw1-5\%}$	7,238				
Lower Grubbs confidence limit (for P=99%)	$x_{minG1-1\%}$	9,52	14,108			
Lower Grubbs confidence limit (for P=95%)	$x_{minG1-5\%}$	9,759	14,164			
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	18,140	19,763	21,167	16,800	14,950	18,517
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	6,784	8,979	#HODNOTA!	8,979	#HODNOTA!
Upper Grubbs confidence limit (for P=99%)	$x_{maxGp-5\%}$	26,521			23,402	
Upper Grubbs confidence limit (for P=95%)	$x_{maxGp-1\%}$	26,760			23,469	
Upper Irwin confidence limit (for P=99%)	$x_{maxlw1-5\%}$	30,662				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	31,708				#HODNOTA!
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	36,450				#HODNOTA!
Standard deviation of a sample	$s_{x,n-1}$	4,8868				
Standard deviation	$s_{x,0}$	4,3709	3,7803	3,0993	4,4576	3,0447
Coefficient of variation	v	26,9%	3,2738	2,5306	3,8604	3,4819
Standard skewness	$Sk_{est}$	-0,222	19,1%	14,6%	26,5%	2,8429
Standard kurtosis (exces)	$\gamma_2$	-1,515	-0,181	0,000	0,249	18,8%
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,776	0,000	0,000	-0,852	0,000
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$	3,747	3,183	#HODNOTA!	3,183	#HODNOTA!
			4,541	#HODNOTA!	4,541	#HODNOTA!

**B1) Tests by Irwin for an afterelimination of outliers**

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,902
	$\lambda_{\text{calc},1,2}$	0,892
	$\lambda_{\text{calc},n,n-1}$	0,263

Value  $x_1$  is not outlier      1 ...  
 Value  $x_p$  is not outlier      1 ...

**Tests by Irwin for an afterelimination of outliers based on a level of significance of 5%**

2,064	2,307	2,064	2,307
0,641	1,857	1,010	1,569
0,351	0,454	1,217	0,845

1      1      1      1

**B2) Tests by Grubb for an afterelimination of outliers or biased values**

Grubb_i=1	$G_1$	1,328	2,146
Grubb_i=p	$G_p$	1,097	1,503
Upper critical values	$G_{h,1\%}$	1,764	1,496

for the Grubb-test  
 according to ISO 5725-2,  
 clause 7.3.4.1

$G_{h,5\%}$	1,715	1,481
	1 ...	0 ..... 0 .....
	1 ...	x1 ** is the outlier xp ** is the outlier

Grubb_i=1,2	$G_{1,2}$	0,335	0,335
Grubb_i=p,p-1	$G_{p,p-1}$	0,324	0,324
Lower critical values	$G_{d,1\%}$	0,002	0,000

for the Grubb-test  
 according to ISO 5725-2,  
 clause 7.3.4.2

$G_{d,5\%}$	0,009	0,000
	1 ...	1 ..... 1 .....
	1 ...	x1 * is the biased value xp * is the biased value

**Test for an afterelimination of one outlier based on a level of significance of 1%**

x1 \*\* is the outlier

**Test for an afterelimination of one biased value based on a level of significance of 5%**

x1 \* is the biased value

xp \* is the biased value

**Test for an afterelimination of two outliers based on a level of significance of 5%**

Values x1, x2 are not outliers

Values xp, xp-1 are not biased values

**Test for an afterelimination of two biased values based on a level of significance of 5%**

Values x1, x2 are not outliers

Values xp, xp-1 are not biased values

**B3) Tests by Dixon for an afterelimination of outliers or biased values**

Dixon_i=1, ... ( $x_2-x_1$ )	$Q_1$	0,329	0,264
Dixon_i=p, ... ( $x_p-x_{(p-1)}$ )	$Q_p$	0,097	0,145
Upper critical values	$Q_{v,a,5\%}$	0,642	0,765

Value  $x_1$  is not biased      1 ...  
 Value  $x_p$  is not biased      1 ...

**Test for an afterelimination of one biased value based on a level of significance of 5%**

0,264	0,803	0,364	0,650
0,145	0,197	0,439	0,350
0,765	0,941	0,765	0,941

1      1      1      1

## Bar chart of frequency distribution for:

## Slag-content - microscopically

