

A) Summary statistics for a sample :

SO3 - content						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 15	14	13	14	13	14
Minimum value	$x_{min} = x_1 = 2,985$	3,17	3,18	2,99	2,99	3,17
Maximum value	$x_{max} = x_p = 3,45$	3,45	3,45	3,44	3,36	3,45
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{max} - x_{min} = 0,465$	0,28	0,27	0,46	0,38	0,28
	$\Delta L_{95\%} = 0,5034$					0,3868
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%} = 2,9647$					3,056
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%} = 3,0210$					3,0998
Lower Irwin confidence limit (for P=95%)	$x_{minlw1-5\%} = 3,0159$					
Lower Grubbs confidence limit (for P=99%)	$x_{minG1-1\%} = 2,9434$	3,0466				
Lower Grubbs confidence limit (for P=95%)	$x_{minG1-5\%} = 3,0088$	3,0688				
Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) = 3,2727$		3,2932	3,3027	3,2600	3,2462	3,2932
Precision of a measure of the mean (for P=95%)	$\pm \epsilon = 0,0673$	0,0703	0,0738	0,0703	0,0738	0,0536
Upper Grubbs confidence limit (for P=99%)	$x_{maxGp-5\%} = 3,5366$			3,5373		
Upper Grubbs confidence limit (for P=95%)	$x_{maxGp-1\%} = 3,602$			3,5648		
Upper Irwin confidence limit (for P=99%)	$x_{maxlw1-5\%} = 3,5941$					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%} = 3,5244$					3,4866
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%} = 3,5807$					3,5304
Standard deviation of a sample	$s_{x,n-1} = 0,11735$	0,0895	0,08553	0,11063	0,10174	0,0895
Standard deviation	$s_{x,0} = 0,11337$	0,08624	0,08217	0,1066	0,09775	0,08624
Coefficient of variation	$v = 3,6\%$	2,7%	2,6%	3,4%	3,1%	2,7%
Standard skewness	$S_k_{est} = -0,700$	0,443	0,456	-0,877	-1,297	0,443
Standard kurtosis (exces)	$\gamma_2 = 1,433$	-0,840	-0,872	2,014	2,770	-0,840
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%} = 2,145$	2,160	2,179	2,160	2,179	2,160
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%} = 2,625$	2,650	2,681	2,650	2,681	2,650

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	1,632
$\lambda_{\text{calc},n,n-1}$	0,088

x_1^{**} 0 ...
Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,383	1,411	1,383	1,411
0,116	0,487	1,735	1,893
0,116	0,122	0,750	0,051

1 1 0 0
1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	2,452
G_p	1,511

Upper critical values

$G_{h,1\%}$	2,806
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for the Grubb-test

1	...
1	...

according to ISO 5725-2,

clause 7.3.4.1	$G_{h,5\%}$	2,249
	0	...
	1	...

Lower critical values

$G_{1,2}$	0,525
$G_{p,p-1}$	0,743

for the Grubb-test

1	...
1	...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1	...
	1	...

Upper critical values

$G_{d,1\%}$	0,253
$G_{d,p-1}$	0,228

for the Grubb-test

1	...
1	...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1	...
	1	...

Lower critical values

$G_{1,2}$	0,525
$G_{p,p-1}$	0,743

for the Grubb-test

1	...
1	...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,337
	1	...
	1	...

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Q_1	0,398
Q_p	0,022

Upper critical values

$Q_{v,a,5\%}$	0,338
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x_1^* is the biased value

0	...
1	...

Value x_p is not biased

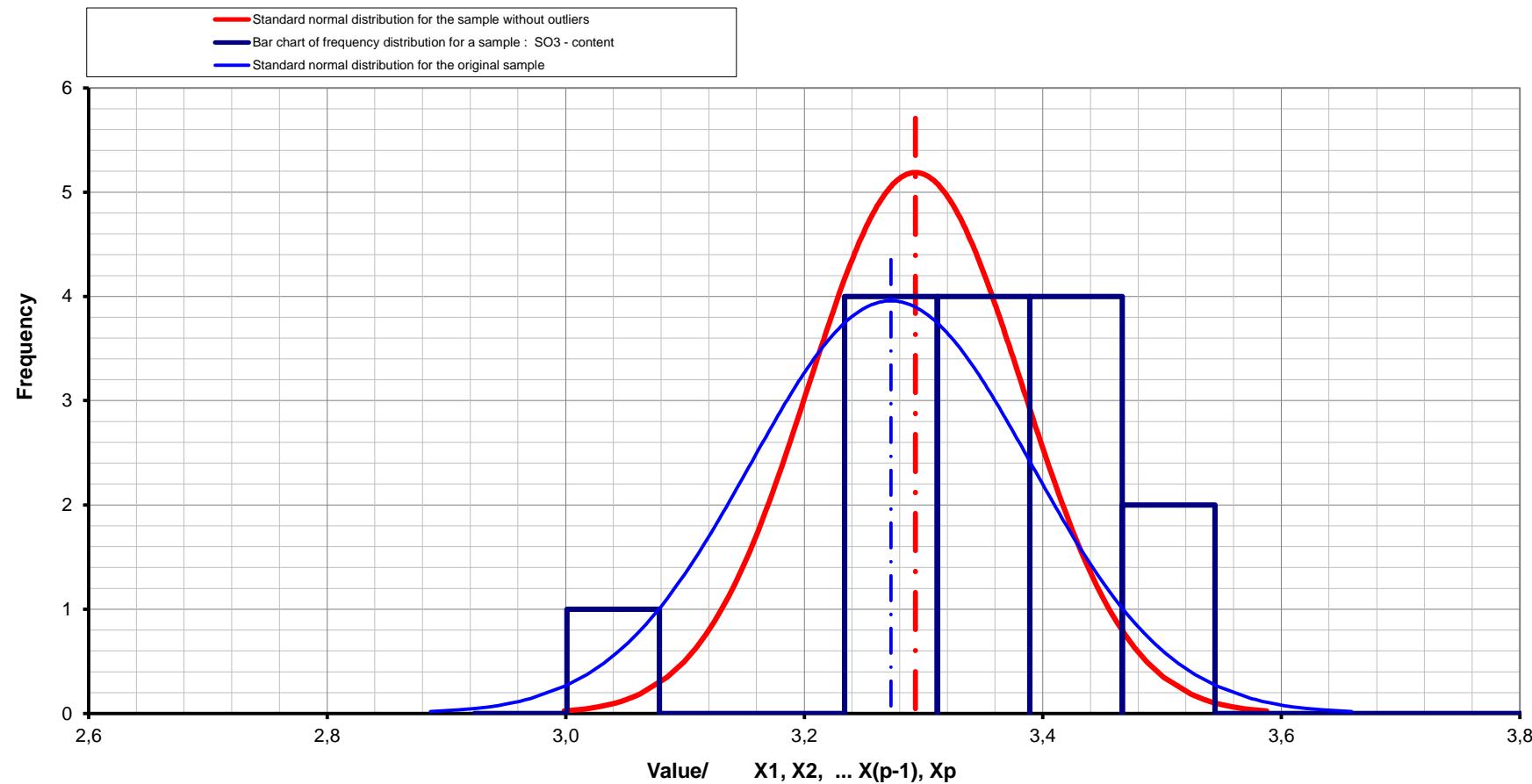
1	...
1	...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,036	0,148	0,407	0,493
0,036	0,037	0,176	0,013

0,349	0,361	0,349	0,361
1	1	1	1

Bar chart of frequency distribution for: SO3 - content



A) Summary statistics for a sample :

CI - content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n = 15					14
Minimum value	$x_{\min} = x_1$ = 0,067		0,08	0,08	0,07	0,08
Maximum value	$x_{\max} = x_p$ = 0,094		0,09	0,09	0,09	0,09
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$ = 0,027		0,02	0,02	0,03	0,02
	$\Delta L_{95\%}$ = 0,028					0,0224
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$ = 0,0650					0,0694
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$ = 0,0681					0,0720
Lower Irwin confidence limit (for P=95%)	$x_{\min l w 1-5\%}$ = 0,0684					
Lower Grubbs confidence limit (for P=99%)	$x_{\min G 1-1\%}$ = 0,0638		0,0689			
Lower Grubbs confidence limit (for P=95%)	$x_{\min G 1-5\%}$ = 0,0674		0,0702			
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} = 0,0821$		0,0832	0,0843	0,0813	0,0805	0,0832
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$ = 0,0037	0,0039	0,0043	0,0039	0,0041	0,0031
Upper Grubbs confidence limit (for P=99%)	$x_{\max G p-5\%}$ = 0,0968			0,096		
Upper Grubbs confidence limit (for P=95%)	$x_{\max G p-1\%}$ = 0,1004			0,0974		
Upper Irwin confidence limit (for P=99%)	$x_{\max l w 1-5\%}$ = 0,1006					
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$ = 0,0961					0,0944
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$ = 0,0992					0,097
Standard deviation of a sample	$s_{x,n-1}$ = 0,00652					
Standard deviation	$s_{x,0}$ = 0,0063	0,00519	0,00486	0,00585	0,00517	0,00519
Coefficient of variation	v = 7,9%	0,005	0,00466	0,00564	0,00497	0,005
Standard skewness	Sk_{est} = -0,257	6,2%	5,8%	7,2%	6,4%	6,2%
Standard kurtosis (exces)	γ_2 = 1,374	0,927	1,046	-0,627	-1,298	0,927
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$ = 2,145	0,130	-0,001	2,247	3,333	0,130
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$ = 2,625	2,160	2,201	2,160	2,179	2,160
		2,650	2,718	2,650	2,681	2,650

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	1,587
$\lambda_{\text{calc},n,n-1}$	0,317

x_1^{**} 0 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,383	1,441	1,383	1,411
0,000	0,215	1,773	2,012
0,400	0,429	0,709	0,402

1	1	0	0
1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	2,316
G_p	1,825

Upper critical values

$G_{h,1\%}$	2,806
for the Grubb-test	1 ...

according to ISO 5725-2,

clause 7.3.4.1

$G_{h,5\%}$	2,249
0 ...	0
1 ...	1

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.1

$G_{1,2}$	0,547
$G_{p,p-1}$	0,622
$G_{d,1\%}$	0,253

Lower critical values

for the Grubb-test

according to ISO 5725-2,

clause 7.3.4.2

$G_{d,5\%}$	0,337
1 ...	1
1 ...	1

Test for an afterelimination of one outlier based on a level of signifiance of 1%

x_1^{**} is the outlier

Value x_p is not outlier

3,121	2,755
2,171	2,507
0	0

Test for an afterelimination of one biased value based on a level of signifiance of 5%

x_1^* is the biased value

Value x_p is not biased

0,547	0,311
0,622	0,311
0,228	0,311

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

1	1
1	1
1	1

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

0,000	0,067	0,400	0,476
0,118	0,133	0,160	0,095
0,349	0,376	0,349	0,361

0 ...	1	0	0
1 ...	1	1	1

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Q_1	0,370
Q_p	0,074

Upper critical values

$Q_{v,a,5\%}$	0,338
x_1^* is the biased value	0 ...

Value x_p is not biased

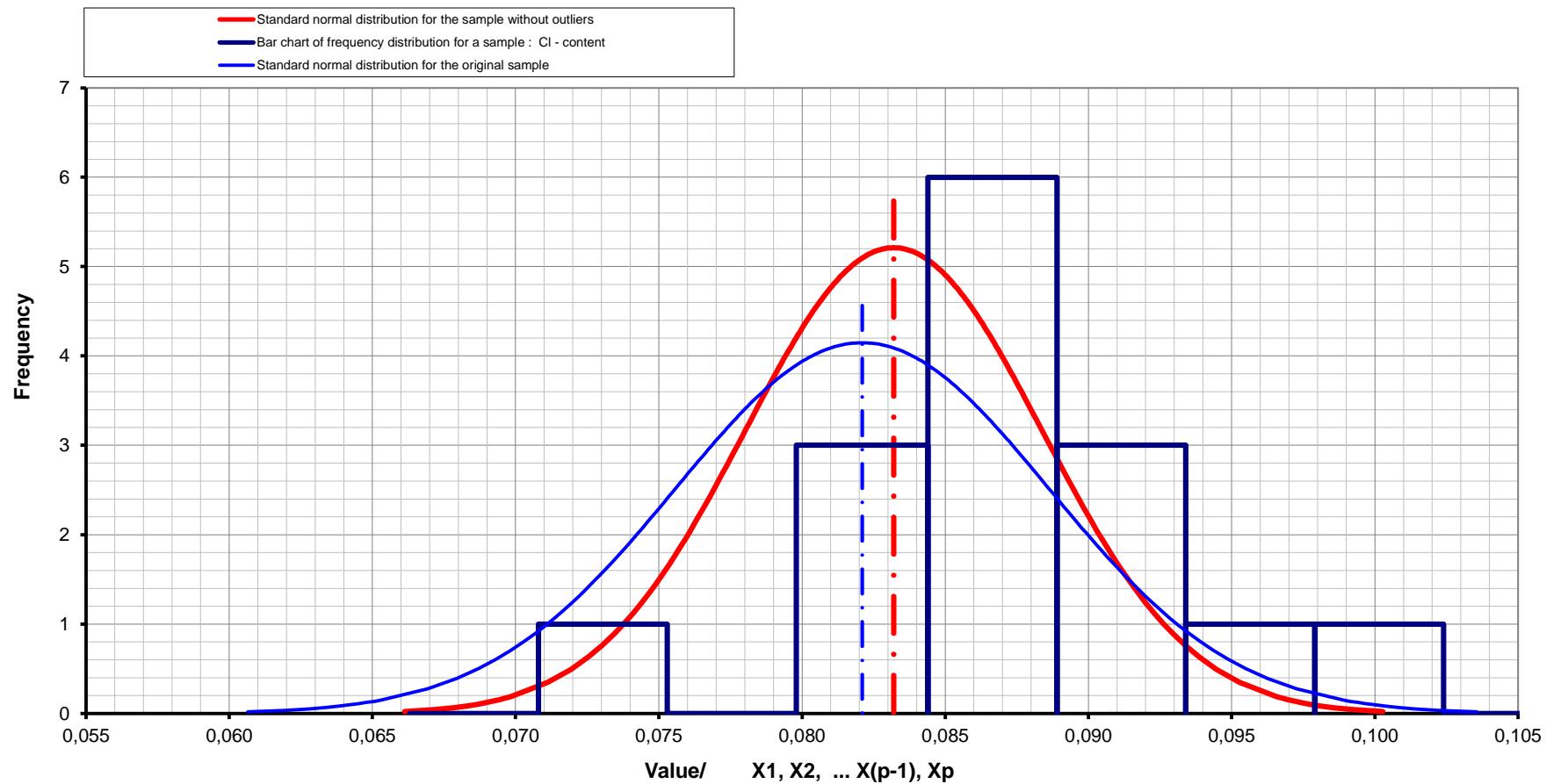
Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,000	0,067	0,400	0,476
0,118	0,133	0,160	0,095
0,349	0,376	0,349	0,361

0 ...	1	0	0
1 ...	1	1	1

Bar chart of frequency distribution for:

CI - content



A) Summary statistics for a sample :

Loss on Ignition						
Count (Sample size)	X ₁ , X ₂ , ... X(p-1), X _p	X ₂ , X ₃ , ... X(p-1), X _p	X ₃ , X ₄ ... X(p-1), X _p	X ₁ , X ₂ , ... X(p-2), X(p-1)	X ₁ , X ₂ , ... X(p-3), X(p-2)	Sample without outliers
n	15	13	12	14	13	14
Minimum value	X _{min} = X ₁	7,615	7,63	7,65	7,62	7,62
Maximum value	X _{max} = X _p	8,52	8,52	8,52	7,97	7,97
Range of sample R = difference L _{m95%} - L _{M95%}	X _{max} - X _{min}	0,905	0,90	0,87	0,36	0,27
	ΔL _{95%}	0,982				0,466
Lower confidence limits after elimination of outliers (for P=98%)	L _{m98%}	7,1819				7,4442
Lower confidence limits after elimination of outliers (for P=95%)	L _{m95%}	7,2917				7,497
	Lower Irwin confidence limit (for P=95%)	7,3244				
	X _{min} lw1-5%	7,1403				
	Lower Grubbs confidence limit (for P=99%)	7,2678				
Precision of a measure of the mean (for P=95%)	Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	7,7827	7,8085	7,8238	7,7300	7,7300
	± ε	0,1312	0,1440	0,1519	0,1372	0,1440
	Upper Grubbs confidence limit (for P=99%)	8,2976			7,9955	
	Upper Grubbs confidence limit (for P=95%)	8,4251			8,0211	
	Upper Irwin confidence limit (for P=99%)	8,2706				
Upper confidence limits after elimination of outliers (for P=95%)	L _{M95%}	8,2737				7,963
Upper confidence limits after elimination of outliers (for P=98%)	L _{M98%}	8,3835				8,0158
Standard deviation of a sample	S _{x,n-1}	0,22893	0,23608	0,23976	0,10785	0,0862
Standard deviation	S _{x,0}	0,22116	0,22682	0,22956	0,10392	0,08282
Coefficient of variation	V	2,9%	3,0%	3,1%	1,4%	1,1%
Standard skewness	S _{k_{est}}	2,668	2,588	2,556	0,959	0,707
Standard kurtosis (exces)	γ ₂	8,232	7,613	7,326	0,290	-0,422
t-value of the Student's distribution for P=95%	t _{(n-1),α=2,5%}	2,145	2,179	2,201	2,160	2,179
t-value of the Student's distribution for P=98%	t _{(n-1),α=1,0%}	2,625	2,681	2,718	2,650	2,681
						2,160

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,359
$\lambda_{\text{calc},1,2}$	0,000
$\lambda_{\text{calc},n,n-1}$	2,487

Value x_1 is not outlier 1 ...
 x_p ** is an outlier 0 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,411	1,441	1,383	1,411
0,110	0,022	0,000	0,000
2,425	2,396	0,818	0,664

1 1 1 1
 0 0 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	0,733
G_p	3,221

Upper critical values

for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.1

Lower critical values

for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.2

$G_{h,1\%}$	2,806
$G_{h,5\%}$	2,249

$G_{1,2}$	1,077
$G_{p,p-1}$	0,140

for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.2

Lower critical values

for the Grubb-test

according to ISO 5725-2,
 clause 7.3.4.2

$G_{d,1\%}$	0,253
$G_{d,5\%}$	0,337

Test for an afterelimination of one outlier based on a level of signifiance of 1%

Value x_1 is not outlier 1
 x_p ** is the outlier 0

Test for an afterelimination of one biased value based on a level of signifiance of 5%

Value x_1 is not biased 1
 x_p * is the biased value 0

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values x_1, x_2 are not outliers 1
 x_p, x_{p-1} * are biased values 0

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values x_1, x_2 are not outliers 1
 x_p, x_{p-1} * are biased values 0

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Dixon_i=p, ... ($x_p - x_{(p-1)}$)

Upper critical values

for the Dixon-test

according to ISO 5725-2,
 clause 7.3.4.2

Lower critical values

for the Dixon-test

according to ISO 5725-2,
 clause 7.3.4.2

Q_1	0,000
Q_p	0,608

Value x_1 is not biased

x_p * is the biased value

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,028 0,006 0,000 0,000

0,615 0,632 0,239 0,204

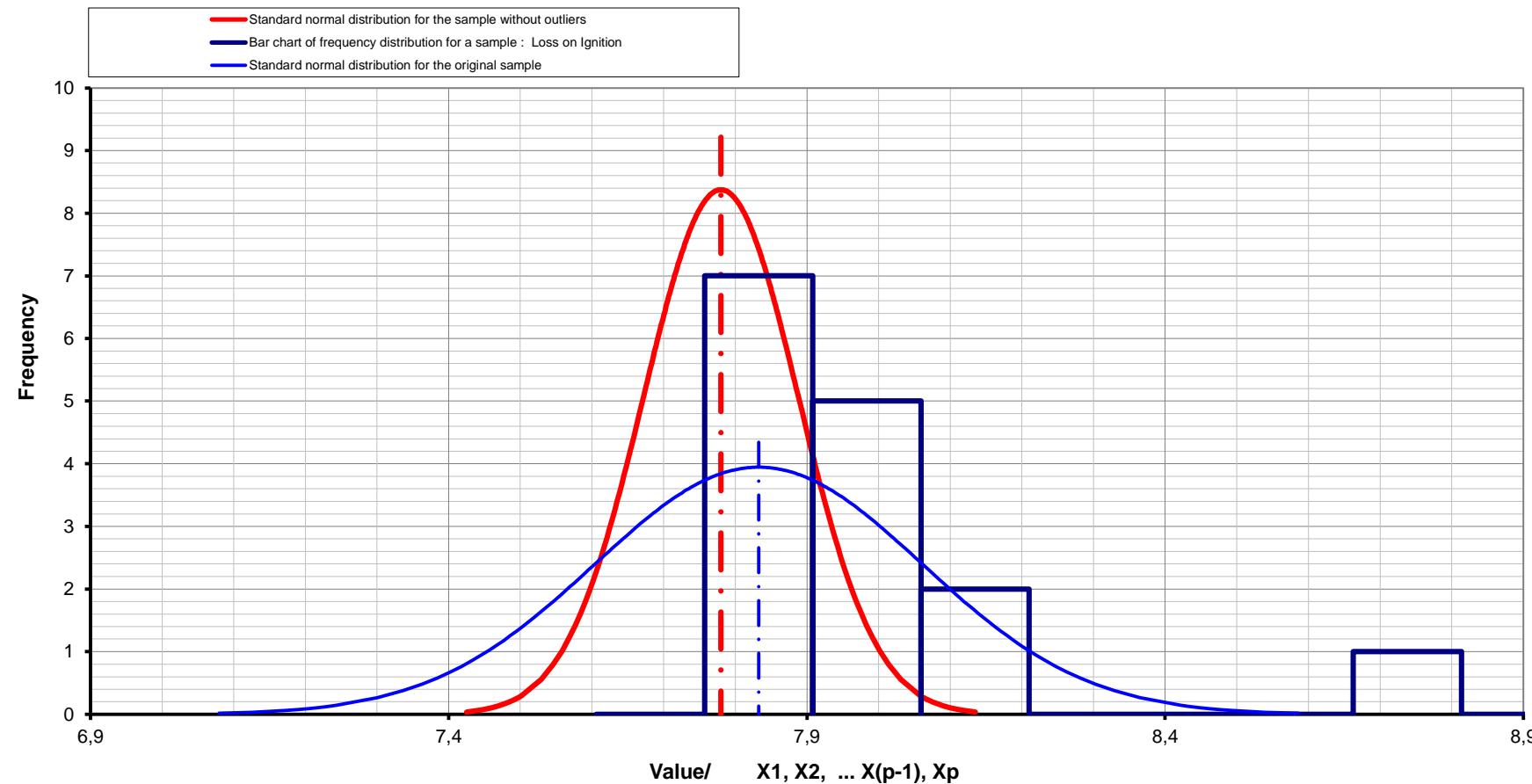
0,361 0,376 0,349 0,361

1 1 1 1

0 0 1 1

Bar chart of frequency distribution for:

Loss on Ignition



A) Summary statistics for a sample :

Insoluble residue						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	14				14
Minimum value	$x_{\min} = x_1$	1,47				1,47
Maximum value	$x_{\max} = x_p$	1,785				1,785
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$	0,315				0,315
	$\Delta L_{95\%}$	0,4522				0,4522
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	1,3672				1,3672
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	1,4185				1,4185
Lower Irwin confidence limit (for P=95%)	$x_{\min l w1-5\%}$	1,3555				1,3555
Lower Grubbs confidence limit (for P=99%)	$x_{\min G1-1\%}$	1,3563				1,3563
Lower Grubbs confidence limit (for P=95%)	$x_{\min G1-5\%}$	1,3822				1,3822
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$		1,6446				1,6446
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0627				0,0627
Upper Grubbs confidence limit (for P=99%)	$x_{\max Gp-5\%}$	1,907				1,907
Upper Grubbs confidence limit (for P=95%)	$x_{\max Gp-1\%}$	1,9329				1,9329
Upper Irwin confidence limit (for P=99%)	$x_{\max l w1-5\%}$	1,9195				1,9195
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	1,8707				1,8707
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	1,9220				1,9220
Standard deviation of a sample	$s_{x,n-1}$	0,10465				0,10465
Standard deviation	$s_{x,0}$	0,10084				0,10084
Coefficient of variation	v	6,4%				6,4%
Standard skewness	Sk_{est}	-0,323				-0,323
Standard kurtosis (exces)	γ_2	-1,067				-1,067
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,160				2,160
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$	2,650				2,650
		2,179	2,201	2,179	2,201	2,160
		2,681	2,718	2,681	2,718	2,650

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,383
	$\lambda_{\text{calc},1,2}$	0,248
	$\lambda_{\text{calc},n,n-1}$	0,050
Value x_1 is not outlier	1 ...	
Value x_p is not outlier	1 ...	

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,411	1,441	1,411	1,441
0,272	0,305	0,259	0,277
0,054	0,061	0,207	0,498

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G_1	1,668	1,969
Grubb_i=p	G_p	1,342	1,505
Upper critical values	$G_{h,1\%}$	2,755	2,699
for the Grubb-test		1 ...	1
according to ISO 5725-2,		1 ...	1
clause 7.3.4.1	$G_{h,5\%}$	2,507	2,462
		1 ...	1
		1 ...	1

Test for an afterelimination of one outlier based on a level of signifiance of 1%

Value x_1 is not outlier

Value x_p is not outlier

Grubb_i=1,2	$G_{1,2}$	0,661	0,661
Grubb_i=p,p-1	$G_{p,p-1}$	0,803	0,803
Lower critical values	$G_{d,1\%}$	0,228	0,202
for the Grubb-test		1 ...	1
according to ISO 5725-2,		1 ...	1
clause 7.3.4.2	$G_{d,5\%}$	0,311	0,284
		1 ...	1
		1 ...	1

Test for an afterelimination of two outliers based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Test for an afterelimination of two biased values based on a level of signifiance of 5%

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

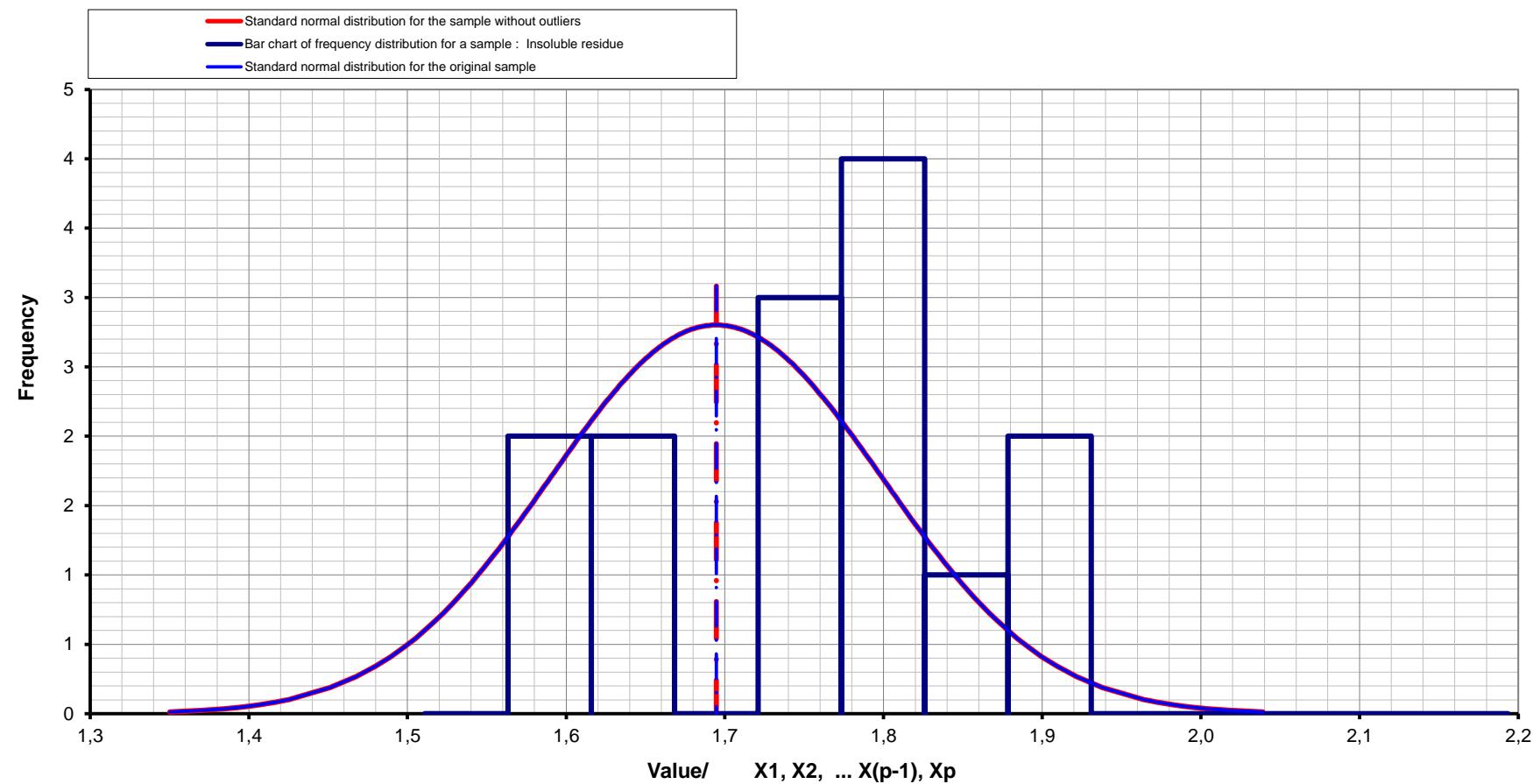
Dixon_i=1, ... (x_2-x_1)	Q_1	0,079	0,086
Dixon_i=p, ... ($x_p-x_{(p-1)}$)	Q_p	0,016	0,017
Upper critical values	$Q_{v,a,5\%}$	0,349	0,361
Value x_1 is not biased		1 ...	1 ...
Value x_p is not biased		1 ...	1 ...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,086	0,094	0,081	0,086
0,017	0,019	0,065	0,155
0,361	0,376	0,361	0,376

Bar chart of frequency distribution for:

Insoluble residue



A) Summary statistics for a sample :

Natriumoxid-content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	13				12
Minimum value	$x_{min} = x_1$	0,21	0,22	0,21	0,21	0,21
Maximum value	$x_{max} = x_p$	0,455	0,46	0,46	0,32	0,32
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{max} - x_{min}$	0,245	0,24	0,24	0,11	0,09
	$\Delta L_{95\%}$	0,2818				0,1608
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	0,1004				0,1595
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,1329				0,1784
	Lower Irwin confidence limit (for P=95%)	0,1273				
	$x_{minlw1-5\%}$	0,0992				
	Lower Grubbs confidence limit (for P=99%)	0,1145				
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n} =$	0,2738	0,2792	0,2850	0,2588	0,2532	0,2588
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0407	0,0429	0,0456	0,0429	0,0456
	Upper Grubbs confidence limit (for P=99%)	0,4331				
	Upper Grubbs confidence limit (for P=95%)	0,4484				
	Upper Irwin confidence limit (for P=99%)	0,4077				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	0,4147				0,3392
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	0,4472				0,3581
Standard deviation of a sample	$s_{x,n-1}$	0,06469				
Standard deviation	$s_{x,0}$	0,06215				
Coefficient of variation	v	23,6%	23,1%	22,6%	14,1%	12,8%
Standard skewness	Sk_{est}	1,927	1,959	2,008	0,129	0,022
Standard kurtosis (exces)	γ_2	4,932	5,040	5,191	-1,264	-1,652
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,179	2,201	2,228	2,201	2,228
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,681	2,718	2,764	2,718	2,764

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,411
$\lambda_{\text{calc},1,2}$	0,080
$\lambda_{\text{calc},n,n-1}$	2,172

Value x_1 is not outlier
 x_p ** is an outlier

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,441	1,477	1,441	1,477
0,081	0,098	0,143	0,161
2,185	2,203	0,572	0,322

1 ...
0 ...
1 ...
0 ...
1 ...
1 ...

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	0,986
G_p	2,801

Upper critical values

for the Grubb-test

according to ISO 5725-2,
clause 7.3.4.1

Lower critical values

for the Grubb-test

according to ISO 5725-2,
clause 7.3.4.2

$G_{h,1\%}$	2,699
1 ...	1

$G_{h,5\%}$	2,462
1 ...	1

$G_{1,2}$	0,972
$G_{p,p-1}$	0,249

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are biased values

$G_{d,1\%}$	0,202
1 ...	1

$G_{d,5\%}$	0,284
1 ...	1

$G_{1,2}$	0,972
$G_{p,p-1}$	0,249

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are biased values

$G_{d,1\%}$	0,174
1 ...	1

$G_{d,5\%}$	0,254
1 ...	1

$G_{1,2}$	0,972
$G_{p,p-1}$	0,249

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Dixon_i=p, ... ($x_p - x_{(p-1)}$)

Upper critical values

for the Dixon-test

according to ISO 5725-2,
clause 7.3.4.2

Q_1	0,020
Q_p	0,551

Value x_1 is not biased

x_p * is the biased value

$Q_{v,a,5\%}$	0,361
1 ...	1

Q_1	0,021
Q_p	0,563

Value x_1 is not biased

x_p * is the biased value

$Q_{v,a,5\%}$	0,376
1 ...	1

Q_1	0,026
Q_p	0,574

Value x_1 is not biased

x_p * is the biased value

$Q_{v,a,5\%}$	0,376
1 ...	1

Q_1	0,045
Q_p	0,182

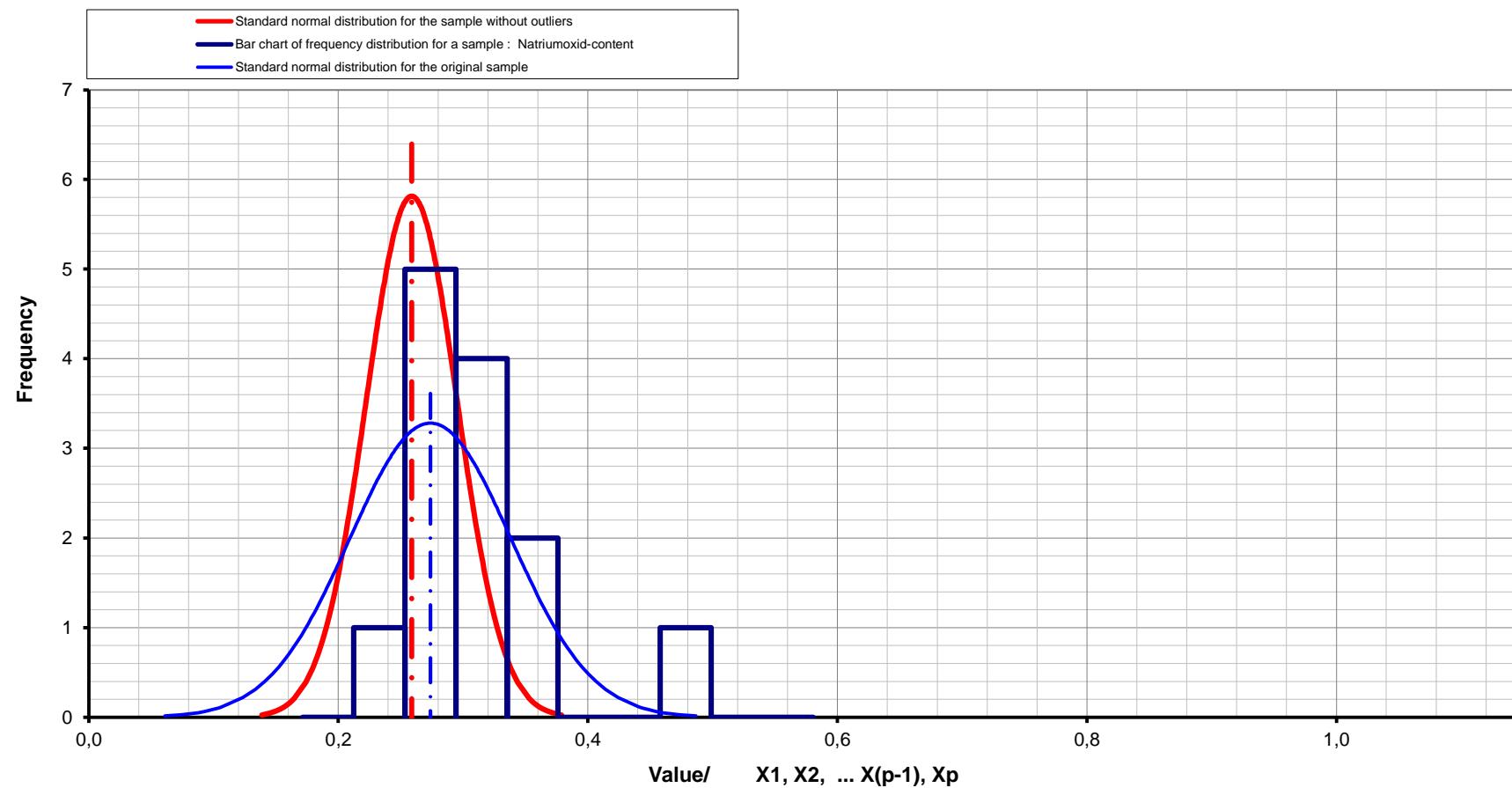
Value x_1 is not biased

x_p * is the biased value

$Q_{v,a,5\%}$	0,392
1 ...	1

Bar chart of frequency distribution for:

Natriumoxid-content



A) Summary statistics for a sample :

Potassiumoxid-content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
n	13					12
Minimum value	$x_{\min} = x_1$	0,586		0,67	0,68	0,67
Maximum value	$x_{\max} = x_p$	0,765		0,77	0,77	0,77
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$	0,179		0,10	0,09	0,17
	$\Delta L_{95\%}$	0,2062				0,128
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	0,5864				0,6447
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,6101				0,6598
	$x_{\min} l_{w1-5\%}$	0,6009				
	$x_{\min} G_{1-1\%}$	0,5855				
	$x_{\min} G_{1-5\%}$	0,5967				
Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	0,7132			0,7238	0,7292	0,7089
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	0,0298		0,0314	0,0333	0,0314
	$x_{\max} G_{p-5\%}$	0,8297				0,0333
	$x_{\max} G_{p-1\%}$	0,8409				0,0193
	$x_{\max} l_{w1-5\%}$	0,8151				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	0,8163				0,7878
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	0,8400				0,8029
Standard deviation of a sample	$s_{x,n-1}$	0,0473				
Standard deviation	$s_{x,0}$	0,04544				
Coefficient of variation	v	6,6%		0,02909	0,02352	0,04665
Standard skewness	Sk_{est}	-1,794		0,02785	0,02243	0,04467
Standard kurtosis (exces)	γ_2	3,801				0,04473
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,179		0,8214		
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,681		0,8319		
			2,201	2,228	2,201	2,228
			2,718	2,764	2,718	2,764
						2,201
						2,718

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)

$\Lambda_{\alpha(n)}$	1,411
$\lambda_{\text{calc},1,2}$	1,739
$\lambda_{\text{calc},n,n-1}$	0,308

x_1^{**} 0 ...
Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,441	1,477	1,441	1,477
0,539	1,337	1,769	1,766
0,503	0,624	0,134	0,000

1 1 0 0
1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1

G_1	2,689
G_p	1,095

4,737
1,203

Upper critical values

$G_{h,1\%}$	2,699
for the Grubb-test	1 ...

Test for an afterelimination of one outlier based on a level of signifiance of 1%

for the Grubb-test

1	...
1	...

x_1^{**} is the outlier
Value x_p is not outlier

according to ISO 5725-2,

clause 7.3.4.1	$G_{h,5\%}$	2,462
	0	...
	1	...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

according to ISO 5725-2,

clause 7.3.4.1	$G_{h,5\%}$	2,462
	0	...
	1	...

x_1^* is the biased value
Value x_p is not biased

Grubb_i=1,2

$G_{1,2}$	0,244
$G_{p,p-1}$	0,969

0,244
0,969

Lower critical values

$G_{d,1\%}$	0,202
for the Grubb-test	1 ...

Test for an afterelimination of two outliers based on a level of signifiance of 5%

for the Grubb-test

1	...
1	...

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,284
	0	...
	1	...

Test for an afterelimination of two biased values based on a level of signifiance of 5%

according to ISO 5725-2,

clause 7.3.4.2	$G_{d,5\%}$	0,284
	0	...
	1	...

Values x_1, x_2 are not outliers

Values x_p, x_{p-1} are not biased values

x_1^*, x_2^* are outliers

Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... ($x_2 - x_1$)

Q_1	0,441
Q_p	0,078

Test for an afterelimination of one biased value based on a level of signifiance of 5%

Dixon_i=p, ... ($x_p - x_{(p-1)}$)

$Q_{p,p-1}$	0,078
$Q_{v,a,5\%}$	0,361

0,150	0,353	0,479	0,497
0,140	0,165	0,036	0,000

x_1^* is the biased value

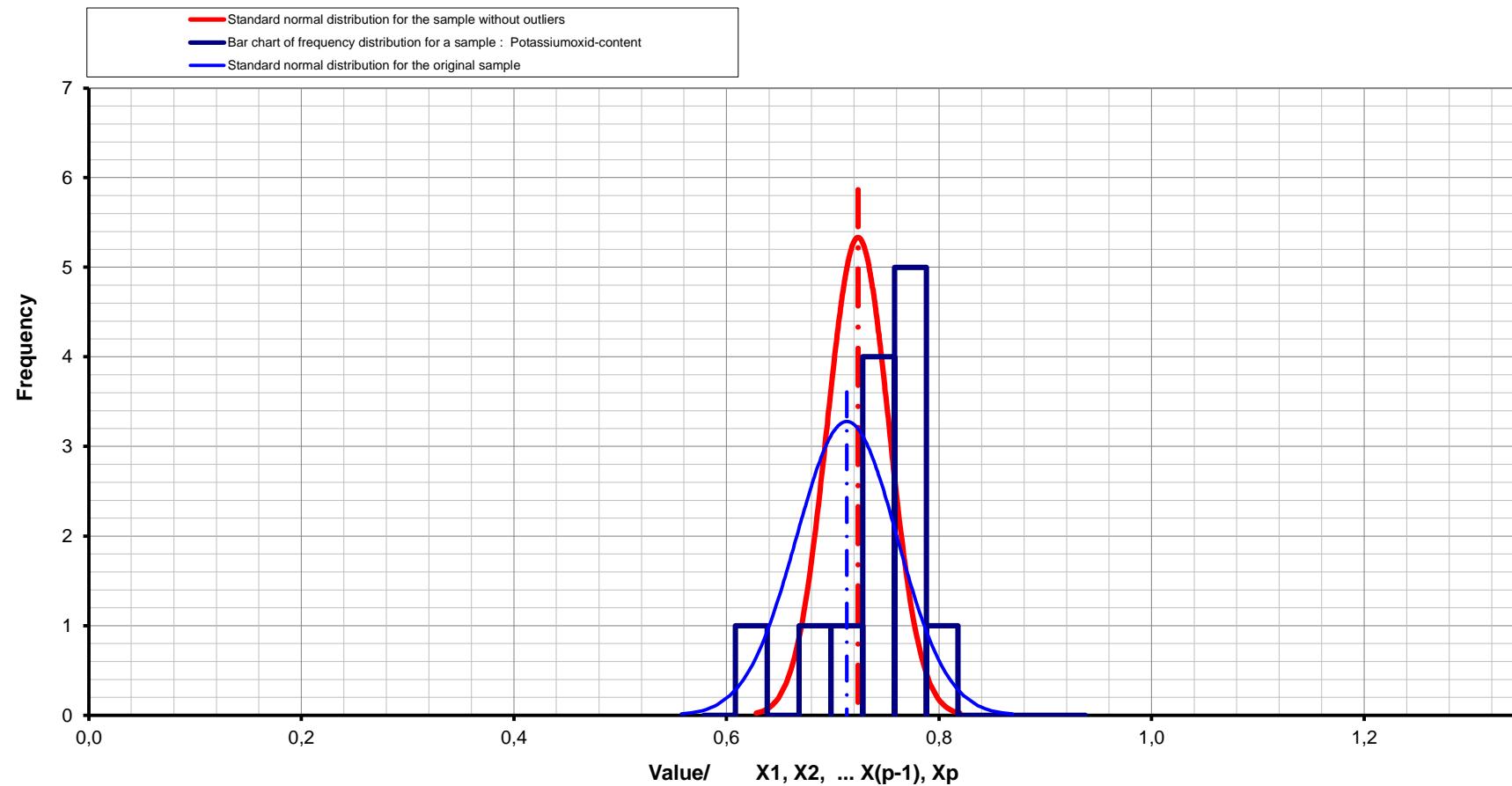
0,376	0,392	0,376	0,392
1	1	1	1

Value x_p is not biased

0	...	0	0
1	1	1	1

Bar chart of frequency distribution for:

Potassiumoxid-content



A) Summary statistics for a sample :

Slag-content - microscopically						
	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	5				3
Minimum value	$x_{\min} = x_1$	11,65				15,55
Maximum value	$x_{\max} = x_p$	23,5				22,35
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$	11,85				6,80
	$\Delta L_{95\%}$	27,136				#HODNOTA!
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	-0,170				#HODNOTA!
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	4,572				#HODNOTA!
Lower Irwin confidence limit (for P=95%)	$x_{\min l w1-5\%}$	7,238				
Lower Grubbs confidence limit (for P=99%)	$x_{\min G1-1\%}$	9,52				
Lower Grubbs confidence limit (for P=95%)	$x_{\min G1-5\%}$	9,759				
Average (arithmetic mean) $\bar{x} = \frac{1/p \sum(x_i)}{n}$		18,140				18,517
Precision of a measure of the mean (for P=95%)	$\pm \epsilon$	6,784				
Upper Grubbs confidence limit (for P=99%)	$x_{\max Gp-5\%}$	26,521				
Upper Grubbs confidence limit (for P=95%)	$x_{\max Gp-1\%}$	26,760				
Upper Irwin confidence limit (for P=99%)	$x_{\max l w1-5\%}$	30,662				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	31,708				#HODNOTA!
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	36,450				#HODNOTA!
Standard deviation of a sample	$s_{x,n-1}$	4,8868				
Standard deviation	$s_{x,0}$	4,3709				
Coefficient of variation	v	26,9%				
Standard skewness	Sk_{est}	-0,222				
Standard kurtosis (exces)	γ_2	-1,515				
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,776				
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1\%}$	3,747				
			3,0993	4,4576	3,0447	3,4819
			2,5306	3,8604	2,486	2,8429
			0,000	0,249	-0,852	0,000
			0,000	0,000	#DELENIENULOU!	0,000
			3,183	#HODNOTA!	3,183	#HODNOTA!
			4,541	#HODNOTA!	4,541	#HODNOTA!

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,902
	$\lambda_{\text{calc},1,2}$	0,892
	$\lambda_{\text{calc},n,n-1}$	0,263
Value x_1 is not outlier	1 ...	
Value x_p is not outlier	1 ...	

Tests by Irwin for an afterelimination of outliers based on a level of significance of 5%

	2,064	2,307	2,064	2,307
	0,641	1,857	1,010	1,569
	0,351	0,454	1,217	0,845
	1	1	1	1
	1	1	1	1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G_1	1,328	2,146
Grubb_i=p	G_p	1,097	1,503
Upper critical values	$G_{h,1\%}$	1,764	1,496
for the Grubb-test		1 ...	0 x1 ** is the outlier
according to ISO 5725-2, clause 7.3.4.1	$G_{h,5\%}$	1,715	1 ... 0 xp ** is the outlier
		1 ...	1,481 Test for an afterelimination of one biased value based on a level of significance of 5%
		1 ...	0 x1 * is the biased value
		1 ...	0 xp * is the biased value
Grubb_i=1,2	$G_{1,2}$	0,335	0,335
Grubb_i=p,p-1	$G_{p,p-1}$	0,324	0,324
Lower critical values	$G_{d,1\%}$	0,002	0,000 Test for an afterelimination of two outliers based on a level of significance of 5%
for the Grubb-test		1 ...	1 Values x1, x2 are not outliers
according to ISO 5725-2, clause 7.3.4.2	$G_{d,5\%}$	0,009	1 ... 1 Values xp, xp-1 are not biased values
		1 ...	0,000 Test for an afterelimination of two biased values based on a level of significance of 5%
		1 ...	1 Values x1, x2 are not outliers
		1 ...	1 Values xp, xp-1 are not biased values

Test for an afterelimination of one outlier based on a level of significance of 1%

x1 ** is the outlier

xp ** is the outlier

Test for an afterelimination of one biased value based on a level of significance of 5%

x1 * is the biased value

xp * is the biased value

Test for an afterelimination of two outliers based on a level of significance of 5%

Values x1, x2 are not outliers

Values xp, xp-1 are not biased values

Test for an afterelimination of two biased values based on a level of significance of 5%

Values x1, x2 are not outliers

Values xp, xp-1 are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

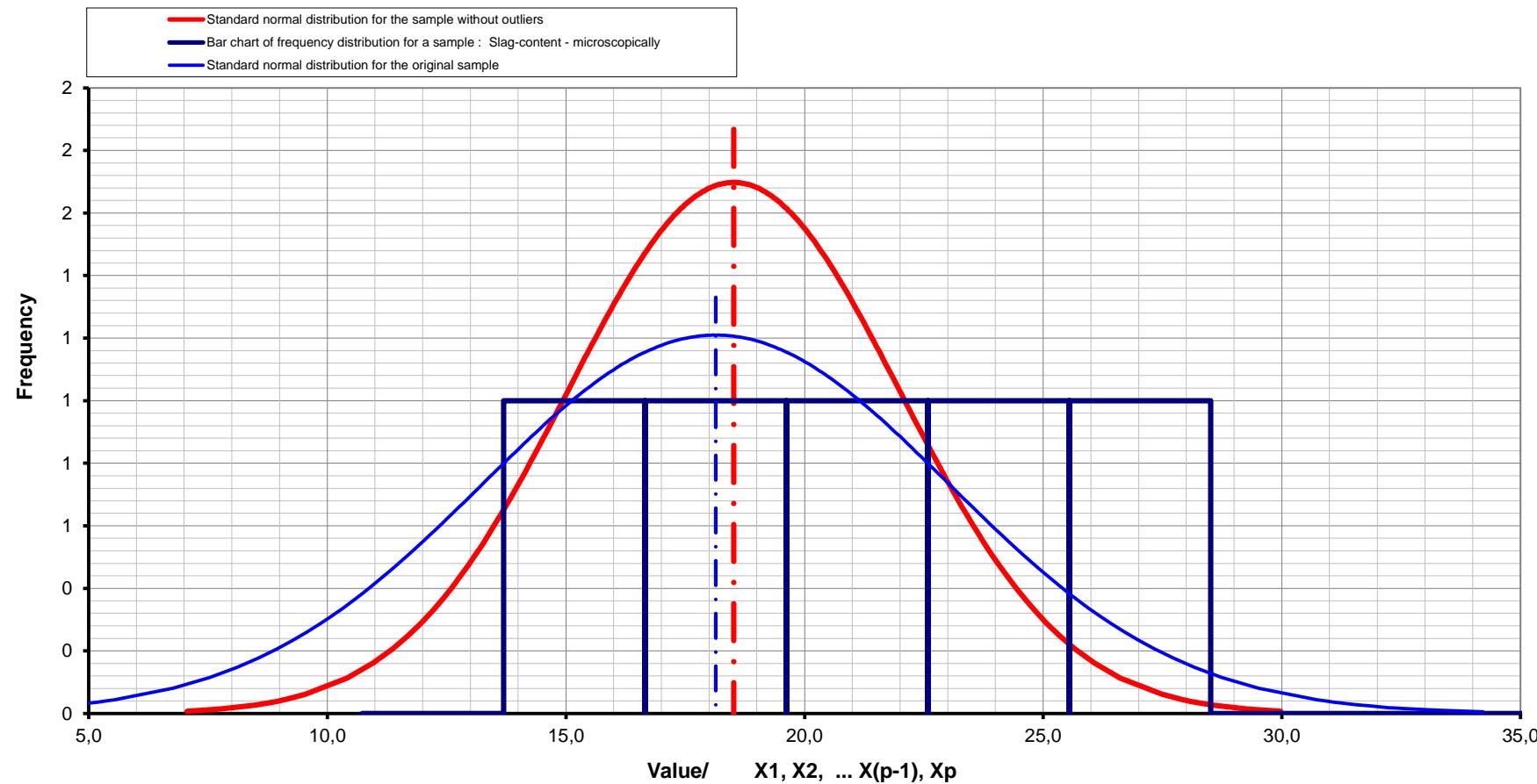
Dixon_i=1, ... (x_2-x_1)	Q_1	0,329	0,264
Dixon_i=p, ... ($x_p-x_{(p-1)}$)	Q_p	0,097	0,145
Upper critical values	$Q_{v,a,5\%}$	0,642	0,765
Value x_1 is not biased	1 ...	1	1
Value x_p is not biased	1 ...	1	1

Test for an afterelimination of one biased value based on a level of significance of 5%

	0,264	0,803	0,364	0,650
	0,145	0,197	0,439	0,350
	0,765	0,941	0,765	0,941
	1	1	1	1
	1	1	1	1

Bar chart of frequency distribution for:

Slag-content - microscopically



A) Summary statistics for a sample :

Cr-content						
Count (Sample size)	X1, X2, ... X(p-1), Xp	X2, X3, ... X(p-1), Xp	X3, X4... X(p-1), Xp	X1, X2, ... X(p-2), X(p-1)	X1, X2, ... X(p-3), X(p-2)	Sample without outliers
Count (Sample size)	n	11				
Minimum value	$x_{\min} = x_1$	1,15				
Maximum value	$x_{\max} = x_p$	5,1				
Range of sample R = difference $L_{m95\%} - L_{M95\%}$	$x_{\max} - x_{\min}$	3,95				
	$\Delta L_{95\%}$	4,924				
Lower confidence limits after elimination of outliers (for P=98%)	$L_{m98\%}$	0,145				
Lower confidence limits after elimination of outliers (for P=95%)	$L_{m95\%}$	0,737				
	Lower Irwin confidence limit (for P=95%)	0,464				
	Lower Grubbs confidence limit (for P=99%)	0,366				
	Lower Grubbs confidence limit (for P=95%)	0,596				
Precision of a measure of the mean (for P=95%)	Average (arithmetic mean) $\bar{x} = \frac{1}{p} \sum (x_i) =$	3,199				
	$\pm \epsilon$	0,779				
	Upper Grubbs confidence limit (for P=99%)	5,802				
	Upper Grubbs confidence limit (for P=95%)	6,032				
	Upper Irwin confidence limit (for P=99%)	5,946				
Upper confidence limits after elimination of outliers (for P=95%)	$L_{M95\%}$	5,661				
Upper confidence limits after elimination of outliers (for P=98%)	$L_{M98\%}$	6,253				
	Standard deviation of a sample $S_{x,n-1}$	1,1051				
	Standard deviation $S_{x,0}$	1,0537				
Coefficient of variation	v	34,5%				
	Standard skewness Sk_{est}	-0,239				
	Standard kurtosis (exces) γ_2	0,236				
t-value of the Student's distribution for P=95%	$t_{(n-1),\alpha=2,5\%}$	2,228				
t-value of the Student's distribution for P=98%	$t_{(n-1),\alpha=1,0\%}$	2,764				
			10	9	10	9
			2,02	2,17	1,15	1,15
			5,10	5,10	4,39	3,65
			3,08	2,93	3,24	2,50
						4,156
						0,812
						1,326
			1,124			
			1,3			
			3,404	3,558	3,009	2,856
			0,833	0,901	0,833	0,901
					5,2	
					5,384	
						5,482
						5,996
			0,9186	0,8266	0,9567	0,8746
			0,8714	0,7793	0,9076	0,8246
			27,0%	23,2%	31,8%	30,6%
			0,217	0,372	-0,752	-1,087
			0,340	1,174	0,182	0,039
			2,262	2,306	2,262	2,306
			2,821	2,897	2,821	2,897
						2,262
						2,821

B1) Tests by Irwin for an afterelimination of outliers

Irwin critical value (for P=95%)	$\Lambda_{\alpha(n)}$	1,477
	$\lambda_{\text{calc},1,2}$	0,826
	$\lambda_{\text{calc},n,n-1}$	0,674

Value x_1 is not outlier 1 ...
 Value x_p is not outlier 1 ...

Tests by Irwin for an afterelimination of outliers based on a level of signifiance of 5%

1,518	1,566	1,518	1,566
0,172	0,962	0,959	1,055
0,815	0,911	0,815	0,182

1 1 1 1

B2) Tests by Grubb for an afterelimination of outliers or biased values

Grubb_i=1	G_1	1,854
Grubb_i=p	G_p	1,720
Upper critical values	$G_{h,1\%}$	2,564

for the Grubb-test
 according to ISO 5725-2,
 clause 7.3.4.1

$G_{h,5\%}$	2,355
1 ...	0 ...
1 ...	1 ...

Grubb_i=1,2	$G_{1,2}$	0,547
Grubb_i=p,p-1	$G_{p,p-1}$	0,612
Lower critical values	$G_{d,1\%}$	0,145

for the Grubb-test
 according to ISO 5725-2,
 clause 7.3.4.2

$G_{d,5\%}$	0,221
1 ...	1 ...
1 ...	1 ...

Test for an afterelimination of one outlier based on a level of signifiance of 1%

2,454	2,186	2,482
1	1	Value x_1 is not outlier
1	0	Value x_p is not outlier

Value x_1 is not outlier
 Value x_p is not outlier
 x_1^* is the biased value
 Value x_p is not biased

Test for an afterelimination of two outliers based on a level of signifiance of 5%

0,547	0,612	0,115
1	1	Values x_1, x_2 are not outliers
1	1	Values x_p, x_{p-1} are not biased values

Values x_1, x_2 are not outliers
 Values x_p, x_{p-1} are not biased values
 Values x_1, x_2 are not outliers
 Values x_p, x_{p-1} are not biased values

B3) Tests by Dixon for an afterelimination of outliers or biased values

Dixon_i=1, ... (x_2-x_1)	Q_1	0,220
Dixon_i=p, ... ($x_p-x_{(p-1)}$)	Q_p	0,180
Upper critical values	$Q_{v,a,5\%}$	0,392

Value x_1 is not biased 1 ...
 Value x_p is not biased 1 ...

Test for an afterelimination of one biased value based on a level of signifiance of 5%

0,049	0,256	0,269	0,348
0,231	0,242	0,228	0,060
0,412	0,437	0,412	0,437

1 1 1 1

Bar chart of frequency distribution for: Cr-content

